gsi.add

## Description

The given operations are performed in parallel for multiple datasets or for two single datasets, or for multiple datasets with a single dataset.

### Usage

```
gsi.add(x,y)
gsi.sub(x,y)
gsi.mul(x,y)
gsi.div(x,y)
```

# Arguments

х	a	vector	or	a	matrix
у	a	vector	or	a	matrix

## Details

All operations +,-,\*,/ are performed on unclassed objects.

### Value

a vector or a matrix with the operated values

# Note

It is better not to use gsi.\* functions directly since they are internal functions of the package

# See Also

```
tmp1 <- matrix(1:12,ncol=3)
tmp2 <- 1:3
gsi.add(tmp1,tmp2)
gsi.sub(tmp1,tmp2)
gsi.mul(tmp1,tmp2)
gsi.div(tmp1,tmp2)
gsi.add(tmp2,tmp2)
gsi.sub(tmp2,tmp2)</pre>
```

```
gsi.mul(tmp2,tmp2)
gsi.div(tmp2,tmp2)
gsi.add(tmp1,tmp1)
gsi.sub(tmp1,tmp1)
gsi.mul(tmp1,tmp1)
gsi.div(tmp1,tmp1)
```

clr

# Centered log ratio transform

## Description

Compute the centered log ratio transform of a (dataset of) composition(s) and its inverse.

## Usage

clr( x )
clr.inv( z )

### Arguments

х	a composition or a data matrix of compositions, not necessarily closed
Z	the clr-transform of a composition or a data matrix of clr-transforms of
	compositions, not necessarily centered (i.e. summing up to zero)

# Details

The clr-transform maps a composition in the D-part Aitchison-simplex isometrically to a D-1 dimensional euclidian vector subspace: consequently, the transformation is not injective and only yields vectors which elements sum up to 0. Thus resulting covariance matrices are always singular.

The data can then be analysed in this transformation by all classical multivariate analysis tools not relying on a full rank of the covariance. See **ilr** and **alr** for alternatives. The interpretation of the results is relatively easy since the relation between each original part and a transformed variable is preserved.

The centered logratio transform is given by

$$clr(x) := \left(\ln x_i - \frac{1}{D}\sum_{j=1}^D \ln x_j\right)_i$$

The image of the clr is given by the vectors with entries summing to 0. This hyperplane is also called the clr-plane.

### Value

clr gives the centered log ratio transform, clr.inv gives closed compositions with the given clr-transforms

## References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

### See Also

ilr,alr,apt

## Examples

```
(tmp <- clr(c(1,2,3)))
clr.inv(tmp)
clr.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(clr(cdata))</pre>
```

gsi.diagGenerate Internal functions: Generate a diagonal matrix

# Description

Generate a diagonal matrix from a vector of the diagonal entries like.

# Usage

gsi.diagGenerate(x)

## Arguments

a vector

## Details

х

The difference to original **diag** is that it always gives a diagonal matrix and does nothing flawed in case of a length one vector.

### Value

a diagonal matrix.

#### Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

gsi.diagExtract, diag

#### Examples

```
diag(1:3)
gsi.diagGenerate(1:3)
gsi.diagGenerate(3)
diag(3)
```

cor.acomp

Correlations of amounts and compositions

## Description

Computes the correlation matrix in the various approaches of compositional and amount data analysis.

## Usage

```
cor(x,y=NULL,...)
## Default S3 method:
cor(x, y=NULL, use="all.obs", method=c("pearson",
"kendall", "spearman"),...)
## S3 method for class 'acomp':
cor(x,y=NULL,...)
## S3 method for class 'rcomp':
cor(x,y=NULL,...)
## S3 method for class 'aplus':
cor(x,y=NULL,...)
## S3 method for class 'rplus':
cor(x,y=NULL,...)
## S3 method for class 'rplus':
cor(x,y=NULL,...)
## S3 method for class 'rmult':
cor(x,y=NULL,...)
```

## Arguments

x	a dataset, eventually of amounts or compositions
У	a second dataset, eventually of amounts or compositions
use	see cor
method	see cor
	further arguments to cor e.g. use

# Details

The correlation matrix does not make much sense for compositions.

In R versions older than v2.0.0, **cor** was defined in package "base" instead of in "stats". This might produce some misfunction.

## Value

The correlation matrix.

## See Also

var.acomp

#### Examples

```
data(SimulatedAmounts)
mean.col(sa.lognormalss)
cor(acomp(sa.lognormals5[,1:3]),acomp(sa.lognormals5[,4:5]))
cor(rcomp(sa.lognormals5[,1:3]),rcomp(sa.lognormals5[,4:5]))
cor(aplus(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
cor(rplus(sa.lognormals5[,1:3]),rplus(sa.lognormals5[,4:5]))
cor(acomp(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
```

segments

Draws straight lines from point to point.

## Description

The function draws lines from a points x to a point y in the given geometry.

## Usage

```
## S3 method for class 'acomp':
segments(x0,y,...,steps=30)
## S3 method for class 'rcomp':
segments(x0,y,...,steps=30)
## S3 method for class 'aplus':
segments(x0,y,...,steps=30)
## S3 method for class 'rplus':
segments(x0,y,...,steps=30)
## S3 method for class 'rmult':
segments(x0,y,...,steps=30)
```

## Arguments

x0	dataset of points of the given type to draw the line from
У	dataset of points of the given type to draw the line to
•••	further graphical parameters
steps	the number of discretisation points to draw the segments not straight on the monitor.

## Details

The functions add lines to the graphics generated with the corresponding plot functions.

Adding to multipaneled plots, redraws the plot completely and is only possible, when the plot has been created with the plotting routines from this library.

## See Also

plot.acomp,lines.acomp

## Examples

data(SimulatedAmounts)

plot(acomp(sa.lognormals))
segments.acomp(acomp(c(1,2,3)),acomp(c(2,3,1)),col="red")
segments.rcomp(acomp(c(1,2,3)),acomp(c(2,3,1)),col="blue")

```
plot(aplus(sa.lognormals[,1:2]))
segments.aplus(aplus(c(10,20)),aplus(c(20,10)),col="red")
segments.rplus(rplus(c(10,20)),rplus(c(20,10)),col="blue")
```

```
plot(rplus(sa.lognormals[,1:2]))
segments.aplus(aplus(c(10,20)),aplus(c(20,10)),col="red")
segments.rplus(rplus(c(10,20)),rplus(c(20,10)),col="blue")
```

matmult

inner product for matrices and vectors

## Description

Multiplies two matrices, if they are conformable. If one argument is a vector, it will be coerced to either a row or a column matrix to make the two arguments conformable. If both are vectors it will return the inner product.

# Usage

```
x %*% y
## S3 method for class 'default':
x %*% y
```

### Arguments

x,y numeric or complex matrices or vectors

# Details

This is a copy of the %% function. The function is made generic to allow the definition of specific methods.

## Value

The matrix product. Uses 'drop' to get rid of dimensions which have only one level.

# See Also

%\*%.rmult

# Examples

M <- matrix(c( 0.2,0.1,0.0, 0.1,0.2,0.0, 0.0,0.0,0.2),byrow=TRUE,nrow=3) x <- c(1,1,2) M %\*% x x %\*% M x %\*% X M %\*% M t(x) %\*% M

cpt

 $Centered \ planar \ transform$ 

# Description

Compute the centered planar transform of a (dataset of) compositions and its inverse.

# Usage

cpt( x )
cpt.inv( z )

### Arguments

х	a composition or a data.matrix of compositions, not necessarily closed
Z	the cpt-transform of a composition or a data matrix of cpt-transforms of
	compositions. It is checked that the z sum up to 0.

## Details

The cpt-transform maps a composition in the D-part real-simplex isometrically to a D-1 dimensional euclidian vector space, identified with a plane parallel to the simplex but passing through the origin. However the transformation is not injective and does not even reach the whole plane. Thus resulting covariance matrices are always singular.

The data can then be analysed in this transformed space by all classical multivariate analysis tools not relying on a full rank of the covariance matrix. See **ipt** and **apt** for alternatives. The interpretation of the results is relitevely easy since the relation of each transformed component to the original parts is preserved.

The centered planar transform is given by

$$cpt(x)_i := clo(x)_i - \frac{1}{D}$$

# Value

cpt gives the centered planar transform, cpt.inv gives closed compositions with the given cpt-transforms.

## References

See Also

clr,apt,ipt

```
(tmp <- cpt(c(1,2,3)))
cpt.inv(tmp)
cpt.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(cpt(cdata))</pre>
```

as.data.frame

## Description

Convert a compositional vector to a dataframe

## Usage

```
## S3 method for class 'acomp':
as.data.frame(x,...)
## S3 method for class 'rcomp':
as.data.frame(x,...)
## S3 method for class 'aplus':
as.data.frame(x,...)
## S3 method for class 'rplus':
as.data.frame(x,...)
## S3 method for class 'rmult':
as.data.frame(x,...)
```

## Arguments

x	an object to be converted to a dataframe
	additional arguments are not used

# Value

a dataframe containing the given data.

# Examples

```
data(SimulatedAmounts)
as.data.frame(acomp(sa.groups))
data.frame(acomp(sa.groups),groups=sa.groups.area)
```

gsi.addclass Internal function: give an object a derived subclass

### Description

This function just extends the class of an object by the given class.

#### Usage

```
gsi.addclass( x , cls)
```

# Arguments

х	The object
cls	the new additional class

# Value

The object **x** with additional class attached.

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

# Examples

gsi.addclass(1:10,"goofy")

gsi.drop

Internal functions: A conditional drop

# Description

drop, if drop is needed.

# Usage

gsi.drop(X,drop)

# Arguments

Х	an array needing dimensions dropped
drop	a logical whether to drop dimensions

# Details

# Value

X or drop(X)

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

drop, gsi

norm

Vector space norm

## Description

Each of the considered space structures has an associated norm, which is computed for each element by these functions.

# Usage

```
norm(x,...)
## Default S3 method:
norm(x,...)
## S3 method for class 'acomp':
norm(x,...)
## S3 method for class 'rcomp':
norm(x,...)
## S3 method for class 'aplus':
norm(x,...)
## S3 method for class 'rplus':
norm(x,...)
## S3 method for class 'rmult':
norm(x,...)
```

## Arguments

x	a dataset or a single vector of some type
	currently not used, intended to select a different norm

# Value

The norms of the given vectors.

# See Also

#### normalize

```
data(SimulatedAmounts)
tmp <- acomp(sa.lognormals)
mvar(tmp)
sum(norm( tmp - mean(tmp) )^2)/(nrow(tmp)-1)</pre>
```

# Description

Computes a power of a positive semidefinite symmetric matrix.

## Usage

```
powerofpsdmatrix( M , p,...)
```

## Arguments

М	a Matrix, preferably symmetric
р	a single number giving the power
	further arguments to the singular value decomposition

## Details

for a symmetric matrix the computed result can actually be considered as a version of the given power of the matrix fullfilling the relation:

 $M^p M^q = M^{p+q}$ 

The symmetry of the matrix is not checked.

# Value

U%\*% D^p %\*% t(P) where the UDP is a singular value decomposition of M.

## References

See Also

```
data(SimulatedAmounts)
d <- ilr(sa.lognormals)
var( d %*% powerofpsdmatrix(var(d),-1/2)) # Unit matrix</pre>
```

princomp.acomp

## Description

A principal component analysis is done in the Aitchison geometry (i.e. clr-transform) of the simplex. Some gimics simplify the interpretation of the computed components as compositional perturbations.

### Usage

```
## S3 method for class 'acomp':
princomp(x,...,scores=TRUE)
## S3 method for class 'princomp.acomp':
print(x,...)
## S3 method for class 'princomp.acomp':
plot(x,y=NULL,...,
npcs=min(10,length(x$sdev)),
type=c("screeplot","variance","biplot","loadings","relative"),
main=NULL,
scale.sdev=1)
## S3 method for class 'princomp.acomp':
predict(object,newdata,...)
```

## Arguments

x	a acomp-dataset (in princomp) or a result from princomp.acomp
У	not used
scores	a logical indicating whether scores should be computed or not
npcs	the number of components to be drawn in the scree plot
type	type of the plot: "screeplot" is a lined screeplot, "variance" is a boxplot like screeplot, "biplot" is a biplot, "loadings" displayes the Loadings as a barplot.acomp
scale.sdev	the multiple of sigma to use plotting the loadings
main	headline of the plot
object	a fitted princomp.acomp object
newdata	another compositional dataset of class acomp
	further arguments to pass to internally-called functions

### Details

As a metric euclidean space the Aitchison simplex has its own principal component analysis, that should be performed in terms of the covariance matrix and not in terms of the meaningless correlation matrix.

To aid the interpretation we added some extra functionality to a normal princomp(clr(x)).

First of all the result contains as additional information the compositional representation of the returned vectors in the space of the data: the center as a composition Center, and the loadings in terms of a composition to perturbe with positively (Loadings) or negatively (DownLoadings). The Up- and DownLoadings are normalized to the number of parts in the simplex and not to one to simplify the interpretation. A value of about one means no change in the specific component. To avoid confusion the meaningless last principal component is removed.

The plot routine provides screeplots (type = "s",type= "v"), biplots (type = "b"), plots of the effect of loadings (type = "b") in scale.sdev\*sdev-spread, and loadings of pairwise (log-)ratios (type = "r").

The interpretation of a screeplot does not differ from ordinary screeplots. It shows the eigenvalues of the covariance matrix, which represent the portions of variance explained by the principal components.

The interpretation of the biplot strongly differs from one. The relevant variables are not the drawn arrows of the components, but rather the links or differences between two arrowheads, which can be interpreted as log-ratios between the two components represented by the arrows.

The compositional loading plot is introduced with this package. The loadings of all component can be seen as an orthogonal basis in the space of clr-transformed data. These vectors are displayed by a barplot with their corresponding composition. For a better interpretation the total of these compositons is set to the number of parts in the composition, such that a portion of one means no effect. This is similar to (but not exactly the same as) a zero loading in a real principal component analysis.

The loadings plot can work in two different modes: if scale.sdev is set to NA it displays the composition beeing represented by the unit vector of loadings in the clr-transformed space. If scale.sdev is numeric we use this composition scaled by the standard deviation of the respective component.

The relative plot displays the **relativeLoadings** as a barplot. The deviation from a unit bar shows the effect of each principal component on the respective ratio.

## Value

princomp gives an object of type c("princomp.acomp","princomp") with the following content:

sdev	the standard deviation of the principal components
loadings	the matrix of variable loadings (i.e., a matrix which columns contain the eigenvectors). This is of class "loadings". The last eigenvector is removed since it should contain the irrelevant scaling.
center	the clr-transformed vector of means used to center the dataset
Center	the acomp vector of means used to center the dataset
scale	the scaling applied to each variable
n.obs	number of observations
scores	if <b>scores</b> = <b>TRUE</b> , the scores of the supplied data on the principal components and the information was available. Scores are coordinates in a basis given by the principal components and thus not compositions
call	the matched call

na.action	not clearly understood
Loadings	compositions that represent a perturbation with the vectors represented by the loadings of each of the factors
DownLoadings	compositions that represent a perturbation with the inverse of the vectors represented by the loadings of each of the factors

predict returns a matrix of scores of the observations in the newdata dataset . The other routines are mainly called for their side effect of plotting or printing and return the object x.

## References

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

Aitchison, J. and M. Greenacre (2002) *Biplots for Compositional Data* Journal of the Royal Statistical Society, Series C (Applied Statistics) **51** (4) 375-392

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

```
http://ima.udg.es/Activitats/CoDaWork03
```

```
http://ima.udg.es/Activitats/CoDaWork05
```

## See Also

clr,acomp, relativeLoadings princomp.aplus, princomp.rcomp, barplot.acomp, mean.acomp,
var.acomp

```
data(SimulatedAmounts)
pc <- princomp(acomp(sa.lognormals5))</pre>
рс
summary(pc)
                   #plot(pc,type="screeplot")
plot(pc)
plot(pc,type="v")
plot(pc,type="biplot")
plot(pc,choice=c(1,3),type="biplot")
plot(pc,type="loadings")
plot(pc,type="loadings",scale.sdev=-1) # Downward
plot(pc,type="relative",scale.sdev=NA) # The directions
plot(pc,type="relative",scale.sdev=1) # one sigma Upward
plot(pc,type="relative",scale.sdev=-1) # one sigma Downward
biplot(pc)
screeplot(pc)
loadings(pc)
```

```
relativeLoadings(pc,mult=FALSE)
relativeLoadings(pc)
relativeLoadings(pc,scale.sdev=1)
relativeLoadings(pc,scale.sdev=2)
```

```
pc$Loadings
pc$DownLoadings
barplot(pc$Loadings)
pc$sdev^2
cov(predict(pc,sa.lognormals5))
```

geometricmean The geometric mean

## Description

Computes the geometric mean.

### Usage

geometricmean(x,...)
geometricmean.row(x,...)
geometricmean.col(x,...)

# Arguments

x	a numeric vector or matrix of data
	further arguments to compute the mean

# Details

The geometric mean is defined as:

$$geometric mean(x) := \left(\prod_{i=1}^n x_i\right)^{1/n}$$

The geometric mean is actually computed by exp(mean(log(c(unclass(x))),...)).

# Value

The geometric means of x as a whole (geometric mean), its rows (geometric mean.row) or its columns (geometric mean.col).

## See Also

mean.rplus

geometricmean(1:10)

acomp

Aitchison compositions

#### Description

A class providing the means to analyse compositions in the philosophical framework of the Aitchison Simplex.

### Usage

acomp(X,parts=1:NCOL(oneOrDataset(X)),total=1)

#### Arguments

Х	composition or dataset of compositions
parts	vector containing the indices xor names of the columns to be used
total	the total amount to be used, typically 1 or 100

#### Details

Many multivariate datasets essentially describe amounts of D different parts in a whole. This has some important implications justifying to regard them as a scale for its own, called a composition. This scale was in-depth analysed by Aitchison (1986) and the functions around the class "acomp" follow his approach.

Compositions have some important properties: Amounts are always positive. The amount of every part is limited to the whole. The absolute amount of the whole is noninformative since it is typically due to artifacts on the measurement procedure. Thus only relative changes are relevant. If the relative amount of one part increases, the amounts of other parts must decrease, introducing spurious anticorrelation (Chayes 1960), when analysed directly. Often parts (e.g H2O, Si) are missing in the dataset leaving the total amount unreported and longing for analysis procedures avoiding spurious effects when applied to such subcompositions. Furthermore, the result of an analysis should be indepent of the units (ppm, g/l, vol.%, mass.%, molar fraction) of the dataset.

From these properties Aitchison showed that the analysis should be based on ratios or log-ratios only. He introduced several transformations (e.g. clr,alr), operations (e.g. perturbe, power.acomp), and a distance (dist) which are compatible with these properties. Later it was found that the set of compositions equiped with perturbations as addition and powertransform as scalar multiplication and the dist as distance form a D-1 dimensional euclidean vector space (Billheimer, Fagan and Guttorp, 2001), which can be mapped isometrically to a usual real vector space by ilr (Pawlowsky-Glahn and Egozcue, 2001).

The general approach in analysing acomp objects is thus to perform classical multivariate analysis on clr/alr/ilr-transformed coordinates and to backtransform or display the results

in such a way that they can be interpreted in terms of the original compositional parts. A side effect of the procedure is to force the compositions to sum up to a *total*, which is done by the closure operation clo.

## Value

a vector of class "acomp" representing one closed composition or a matrix of class "acomp" representing multiple closed compositions each in one row.

#### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

Billheimer, D., P. Guttorp, W.F. and Fagan (2001) Statistical interpretation of species composition, *Journal of the American Statistical Association*, **96** (456), 1205-1214

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

Pawlowsky-Glahn, V. and ??? (2003) ???

http://ima.udg.es/Activitats/CoDaWork03

http://ima.udg.es/Activitats/CoDaWork05

## See Also

clr,rcomp, aplus, princomp.acomp, plot.acomp, boxplot.acomp, barplot.acomp, mean.acomp, var.acomp, variation.acomp, cov.acomp, msd

#### Examples

```
data(SimulatedAmounts)
plot(acomp(sa.lognormals))
```

rcomparithm

Arithmetic operations for composition in real geometry

## Description

The real compositions form a manifold of real vector space. The induced operations +,-,\*,/ give results valued in the real vector space, but possibly outside the simplex.

### Usage

```
convex.rcomp(x,y,alpha=0.5)
## Methods for class "rcomp"
## x+y
## x-y
## -x
## -x
## x*r
## r*x
## r*x
## x/r
```

### Arguments

х	an rcomp composition or dataset of compositions
У	an rcomp composition or dataset of compositions
r	a numeric vector of size 1 or $nrow(x)$
alpha	a numeric vector of size 1 or $\operatorname{nrow}(x)$ with values between 0 and 1

# Details

The functions behave quite like +.rmult. The convex combination is defined as: x\*alpha + (1-alpha)\*y

## Value

rmult-objects containing the given operations on the simplex as subset of the  $R^D$ . Only the convex combination convex.rcomp results in an rcomp-object again, since only this operation is closed.

# Note

For \* the arguments x and y can be exchanged.

## See Also

+.rmult, +.acomp,cpt, rcomp, rmult

```
rcomp(1:5)* -1 + rcomp(1:5)
data(SimulatedAmounts)
cdata <- rcomp(sa.lognormals)
plot( tmp <- (cdata-mean(cdata))/msd(cdata) )
class(tmp)
mean(tmp)
msd(tmp)
var(tmp)
plot(convex.rcomp(rcomp(c(1,1,1)),sa.lognormals,0.1))</pre>
```

Hydrochem

## Description

Contains the hydrochemical compositional data set obtained from several rivers in the Llobregat river basin, in northeastern Spain.

## Usage

data(Hydrochem)

## Format

Data matrix with 485 cases and 19 variables.

#### Details

This hydrochemical data set contains measurements of 14 components, H, Na, K, Ca, Mg, Sr, Ba, NH<sub>4</sub>, Cl, HCO<sub>3</sub>, NO<sub>3</sub>, SO<sub>4</sub>, PO<sub>4</sub>, TOC. From them, hydrogen was derived by inverting the relationship between its stable form in water,  $H_3O^+$ , and pH. Details can be found in Otero et al. (2005). Each of these parameters is measured approximately once each month during 2 years in 31 stations, placed along the rivers and main tributaries of the Llobregat river, one of the medium rivers in northeastern Spain.

The Llobregat river drains an area of 4948.2  $km^2$ , and it is 156.6 km long, with two main tributaries, Cardener and Anoia. The headwaters of Llobregat and Cardener are in a rather unpolluted area of the Eastern Pyrenees. Mid-waters these rivers flow through a densely populated and industrialized area, where potash mining activity occurs and there are large salt mine tailings stored with no water proofing. There, the main land use is agriculture and stockbreeding. The lower course flows through one of the most densely populated areas of the Mediterranean region (around the city of Barcelona) and the river receives large inputs from industry and urban origin, while intensive agriculture activity is again present in the Llobregat delta. Anoia is quite different. Its headwaters are in an agricultural area, downwaters it flows through an industrialized zone (paper mills, tannery and textile industries), and near the confluence with Llobregat the main land use is agriculture again, mainly vineyards, with a decrease in industry and urban contribution. Given this variety in geological background and human activities, the sample has been splitted in four groups (higher Llobregat course, Cardener, Anoia and lower Llobregat course), which in turn are splitted into main river and tributaries (Otero et al. 2005). Information on these groupings, the sampling locations and sampling time is included in 5 complementary variables.

### Source

The datasets are also accessible in Otero et al. (2005), and are here included under the GNU Public Library Licence Version 2 or newer.

### References

Otero, N.; R. Tolosana-Delgado, A. Soler, V. Pawlowsky-Glahn and A. Canals (2005). Relative vs. absolute statistical analysis of compositions: A comparative study of surface waters of a Mediterranean river. Water Research, in press. doi: 10.1016/j.watres.2005.01.012

# Examples

data(Hydrochem) biplot(princomp(rplus(Hydrochem))) biplot(princomp(rcomp(Hydrochem))) biplot(princomp(aplus(Hydrochem))) biplot(princomp(acomp(Hydrochem)))

straight

## Draws infinite straight lines.

## Description

The function draws lines in a given direction d through points x.

### Usage

```
straight(x,...)
## S3 method for class 'acomp':
straight(x,d,...,steps=30)
## S3 method for class 'rcomp':
straight(x,d,...,steps=30)
## S3 method for class 'aplus':
straight(x,d,...,steps=30)
## S3 method for class 'rplus':
straight(x,d,...,steps=30)
## S3 method for class 'rmult':
straight(x,d,...,steps=30)
```

# Arguments

x	dataset of points of the given type to draw the line through
d	dataset of directions of the line
	further graphical parameters
steps	the number of discretisation points to draw the segments not straight on the monitor.

## Details

The functions add lines to the graphics generated with the corresponding plot functions. Adding to multipaneled plots, redraws the plot completely and is only possible, when the plot has been created with the plotting routines from this library.

Lines end, when they leave the space (e.g. the simplex), which sometimes leads to the impression of premature end.

## See Also

plot.acomp,lines.acomp

### Examples

data(SimulatedAmounts)

```
plot(acomp(sa.lognormals))
straight(mean(acomp(sa.lognormals)),princomp(acomp(sa.lognormals))$Loadings[1,],col="red")
straight(mean(rcomp(sa.lognormals)),princomp(rcomp(sa.lognormals))$loadings[,1],col="blue")
```

```
plot(aplus(sa.lognormals[,1:2]))
straight(mean(aplus(sa.lognormals[,1:2])),princomp(aplus(sa.lognormals[,1:2]))$Loadings[1,],col="red")
straight(mean(rplus(sa.lognormals[,1:2])),princomp(rplus(sa.lognormals[,1:2]))$loadings[,1],col="blue")
```

```
plot(rplus(sa.lognormals[,1:2]))
straight(mean(aplus(sa.lognormals[,1:2])),princomp(aplus(sa.lognormals[,1:2]))$Loadings[1,],col="red")
straight(mean(rplus(sa.lognormals[,1:2])),princomp(rplus(sa.lognormals[,1:2]))$loadings[,1],col="blue")
```

ratioLoadings

Loadings of relations of two amounts

#### Description

In a compositional dataset the relation of two objects can be interpreted better than a single amount. These functions compute, display and plot the corresponding pair-information for the various principal component analysis results.

#### Usage

```
relativeLoadings(x,...)
## S3 method for class 'princomp.acomp':
relativeLoadings(x,...,log=FALSE,scale.sdev=NA,cutoff=0.1)
## S3 method for class 'princomp.aplus':
relativeLoadings(x,...,log=FALSE,scale.sdev=NA,cutoff=0.1)
## S3 method for class 'princomp.rcomp':
relativeLoadings(x,...,scale.sdev=NA,cutoff=0.1)
## S3 method for class 'princomp.rplus':
```

```
relativeLoadings(x,...,scale.sdev=NA,cutoff=0.1)
## S3 method for class 'relativeLoadings.princomp.acomp':
print(x,...,cutoff=attr(x,"cutoff"),
                                                  digits=2
                                                  )
## S3 method for class 'relativeLoadings.princomp.aplus':
print(x,...,cutoff=attr(x,"cutoff"),
                                                  digits=2
                                                  )
## S3 method for class 'relativeLoadings.princomp.rcomp':
print(x,...,cutoff=attr(x,"cutoff"),
                                                  digits=2
                                                  )
## S3 method for class 'relativeLoadings.princomp.rplus':
print(x,...,cutoff=attr(x,"cutoff"),
                                                  digits=2
                                                  )
## S3 method for class 'relativeLoadings.princomp.acomp':
plot(x,...)
## S3 method for class 'relativeLoadings.princomp.aplus':
plot(x,...)
## S3 method for class 'relativeLoadings.princomp.rcomp':
plot(x,...)
## S3 method for class 'relativeLoadings.princomp.rplus':
plot(x,...)
```

# Arguments

x	$a\ result\ from\ an\ amount\ PCA\ \texttt{princomp.acomp}/\texttt{princomp.aplus}/\texttt{princomp.rcomp}/\texttt{princomp.rcomp}/\texttt{princomp.rcomp}/\texttt{princomp.rcomp}/\texttt{princomp}/prin$
log	a logical indicating to use log-ratios instead of ratios
scale.sdev	If not NA, a number specifying the multiple of a standard deviation the component is to be multiplied with.
cutoff	A single number. Changes under that (log)-cutoff are not displayed.
digits	The number of digits to be displayed
	further parameters to internally-called functions

# Details

The relative loadings of components allow a direct interpretation of the effects of principal components. For acomp/aplus classes the relation is induced by a ratio, which can optionally be log-transformed. For the rcomp/rplus-classes the relation is induced by a difference, which is quite meaningless when the units are different.

## Value

The value is a matrix of type "relativeLoadings.princomp.\*", containing the ratios in the compositions represented by the loadings (optionally scaled by the standard deviation of the components and scale.sdev).

# See Also

```
princomp.acomp, princomp.aplus, barplot
```

## Examples

```
data(SimulatedAmounts)
pc <- princomp(acomp(sa.lognormals5))
pc
summary(pc)
relativeLoadings(pc,log=TRUE)
relativeLoadings(pc)
relativeLoadings(pc,scale.sdev=1)
relativeLoadings(pc,log=TRUE))
plot(relativeLoadings(pc))
plot(relativeLoadings(pc,scale.sdev=1))
plot(relativeLoadings(pc,scale.sdev=2))</pre>
```

gsiinternal1 Internal functions of the compositions package

#### Description

Internal functions

## Usage

gsi.closespread(spread)

### Arguments

spread

# Details

# Value

like spread but projected to the orthognonal complement of  $c(1, \ldots, 1)$ 

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi

gsi.simshape Internal function: Reshape an object to the shape type of another

# Description

Reshape an object to the shape type of another

# Usage

gsi.simshape(x,oldx)

# Arguments

х	the data to be returned
oldx	a data of the intended shape

# Details

## Value

**x** is shaped as old**x** 

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

## References

See Also

# Examples

gsi.simshape(matrix(1:4,nrow=1),1:3)

# Description

Calculates a distance matrix from a dataset.

# Usage

dist(x,...)
## Default S3 method:
dist(x,...)

# Arguments

x	a dataset
	further arguments to ${\tt dist}$

## Details

The distance is computed based on cdt

## Value

a distance matrix

# See Also

aplus

# Examples

```
data(iris)
dist(iris[,1:4])
data(SimulatedAmounts)
dist(acomp(sa.lognormals),method="manhattan")
dist(rcomp(sa.lognormals))
dist(aplus(sa.lognormals))
dist(rplus(sa.lognormals))
```

### dist

summary.aplus

## Description

## Usage

```
## S3 method for class 'aplus':
summary( object, ...,digits=max(3, getOption("digits")-3))
## S3 method for class 'rplus':
summary( object, ...)
## S3 method for class 'rmult':
summary( object, ...)
```

# Arguments

object	an aplus/rplus set of amounts
digits	the number of significant digits to be used. The argument can also be used with rplus/rmult.
	not used, only here for generics

# Details

## Value

A matrix containing summary statistics. The obtained value is the same as for the classical summary summary, although in the case of aplus objects, the statistics have been computed in a logarithmic geometry and exponentiated.

## References

# See Also

aplus, rplus, summary. acomp, summary. rcomp

```
data(SimulatedAmounts)
summary(aplus(sa.lognormals))
summary(rplus(sa.lognormals))
summary(rmult(sa.lognormals))
```

### Description

Compute the metric variance, covariance, correlation or standard deviation.

### Usage

```
mvar(x,...)
mcov(x,...)
mcor(x,...)
msd(x,...)
mvar.default(x,y=NULL,...)
mcov.default(x,y=x,...)
mcor.default(x,y,...)
msd.default(x,y=NULL,...)
```

### Arguments

х	a dataset, eventually of amounts or compositions
У	a second dataset, eventually of amounts or compositions
•••	further arguments to var or cov e.g. use

# Details

The metric variance (mvar) is defined by the trace of the variance in the natural geometry of the data, or also by the generalized variance in natural geometry. The natural geometry is equivalently given by the cdt or idt transforms.

The metric standard deviation (msd) is not the square root of the metric variance, but the square root of the mean of the eigenvalues of the variance matrix. In this way it can be interpreted in units of the original natural geometry, as the diameter of a 1-sigma sperical ball around the mean.

The metric covariance (mvar) is the sum over the absolute singular values of the covariance of two datasets in their respective geometries. It is always positive. The metric covariance of a dataset with itself is its metric variance. The interpretation of a metric covariance is quite difficult.

The metric correlation (mcor) is the metric covariance of the datasets in their natural geometry normalized to unit variance matrix. It is a number between 0 and the smaller dimension of both natural spaces. A number of 1 means perfect correlation in 1 dimension, but only partial correlations in higher dimensions.

# mvar

## Value

a scalar number, informing of the degree of variation/covariation of one/two datasets.

#### References

Daunis-i-Estadella, J., J.J. Egozcue, and V. Pawlowsky-Glahn (2002) Least squares regression in the Simplex on the simplex, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

### See Also

var, cov, mean.acomp, acomp, rcomp, aplus, rplus

## Examples

```
data(SimulatedAmounts)
mvar(acomp(sa.lognormals))
mvar(rcomp(sa.lognormals))
mvar(aplus(sa.lognormals))
mvar(rplus(sa.lognormals))
msd(acomp(sa.lognormals))
msd(rcomp(sa.lognormals))
msd(aplus(sa.lognormals))
msd(rplus(sa.lognormals))
mcov(acomp(sa.lognormals5[,1:3]),acomp(sa.lognormals5[,4:5]))
mcor(acomp(sa.lognormals5[,1:3]),acomp(sa.lognormals5[,4:5]))
mcov(rcomp(sa.lognormals5[,1:3]),rcomp(sa.lognormals5[,4:5]))
mcor(rcomp(sa.lognormals5[,1:3]),rcomp(sa.lognormals5[,4:5]))
mcov(aplus(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
mcor(aplus(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
mcov(rplus(sa.lognormals5[,1:3]),rplus(sa.lognormals5[,4:5]))
mcor(rplus(sa.lognormals5[,1:3]),rplus(sa.lognormals5[,4:5]))
mcov(acomp(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
mcor(acomp(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
```

```
boxplot
```

Displaying compositions and amounts by boxplots

#### Description

For the different interpretations of amount data a different type of boxplot is feasible. Thus different boxplots are drawn.

## Usage

# Arguments

X	a dataset
fak	a factor to split the dataset, not yet implemented in aplus and rplus
xlim	x-limits of the plot
ylim	y-limits of the plot
log	logical indicating whether ploting should be done on log scale
panel	the panel function to be used or a list of multiple panel functions
	further graphical parameters
dots	a logical indicating whether the points should be drawn
boxes	a logical indicating the boxes should be drawn
У	used by pairs
notch	should the boxes be notched

# Details

vp.boxplot and vp.logboxplot are only used as panel functions.

#### See Also

plot.acomp, qqnorm.acomp

```
data(SimulatedAmounts)
boxplot(acomp(sa.lognormals))
boxplot(rcomp(sa.lognormals))
boxplot(aplus(sa.lognormals))
boxplot(rplus(sa.lognormals))
```

ellipses

### Description

Draws ellipses from a mean and a variance into a plot.

## Usage

```
ellipses(mean,...)
## S3 method for class 'acomp':
ellipses(mean,var,r=1,...,steps=360)
## S3 method for class 'rcomp':
ellipses(mean,var,r=1,...,steps=360)
## S3 method for class 'aplus':
ellipses(mean,var,r=1,...,steps=360)
## S3 method for class 'rplus':
ellipses(mean,var,r=1,...,steps=360)
## S3 method for class 'rmult':
ellipses(mean,var,r=1,...,steps=360)
```

## Arguments

mean	a dataset/value of means or midpoints of the ellipses
var	a variance matrix or a set of variance matrices given by <b>var[i,,]</b> . The principle axis of the variance give the axis of the ellipses. The the square-root of the eigenvalues times r give the large and small halfdiameter of the ellipse.
r	A scaling of the radius
	further graphical parameters
steps	the numer of discretisation points to draw the ellipses.

## Details

The ellipse drawn is given by the solutions of

 $(x - mean)^t var^{-1}(x - mean) = r^2$ 

in the respective geometry of the parameter space. Currently the compositional scales (acomp and rcomp) can be used only for three part compositions and plot into a ternary diagram and the not sum constrained scales (aplus, rplus and rmult) can only be used with two parts and draw into any scatterplot.

TODO: Adding to multi-panel plots

### See Also

plot.acomp,

```
data(SimulatedAmounts)
plot(acomp(sa.lognormals))
tt<-acomp(sa.lognormals); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rcomp(sa.lognormals[,1:2]))
tt<-aplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-aplus(sa.lognormals[,1:2]))
tt<-aplus(sa.lognormals[,1:2]))
tt<-aplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")</pre>
```

```
meanrow
```

The arithmetic mean of rows or columns

# Description

Computes the arithmetic mean.

#### Usage

mean.row(x,..., na.action=get(getOption("na.action")))
mean.col(x,..., na.action=get(getOption("na.action")))

## Arguments

x	a numeric vector or matrix of data
	arguments to mean
na.action	The na.action to be used: one of na.omit,na.fail,na.pass

# Details

# Value

The arithmetic means of the rows (mean.row) or columns (mean.col) of x.

## See Also

mean.rplus

```
data(SimulatedAmounts)
mean.col(sa.tnormals)
mean.row(sa.tnormals)
```

gsi.margin

Internal function: Compute a desired compositional margin

# Description

This generic function should select the selected type of margin based on the class of the dataset and the specified margin type.

## Usage

```
gsi.margin(X,...)
gsi.margin.acomp(X,what,...,margin="acomp")
gsi.margin.rcomp(X,what,...,margin="rcomp")
gsi.margin.aplus(X,what,...)
gsi.margin.rplus(X,what,...)
```

# Arguments

Х	The dataset to take the margin from.
what	The indices xor column names to be kept.
margin	The type of marginalisation to be used. Possible values are: "sub", "rcomp", "acomp" and an index xor a name of a variable in the dataset.
	other arguments

# Details

# Value

Some marginal dataset or vector still containing the variables given by what and optionally one additional part named "+", "\*" or margin.

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

gsi

```
data(SimulatedAmounts)
plot(gsi.margin(acomp(sa.lognormals5),c("Cd","Cu")))
```

barplot.acomp Barcharts of amounts

# Description

Compositions and amounts can

## Usage

```
## S3 method for class 'acomp':
barplot(height,...,legend.text=TRUE,beside=FALSE,total=1)
## S3 method for class 'rcomp':
barplot(height,...,legend.text=TRUE,beside=FALSE,total=1)
## S3 method for class 'aplus':
barplot(height,...,legend.text=TRUE,beside=TRUE)
## S3 method for class 'rplus':
barplot(height,...,legend.text=TRUE,beside=TRUE)
```

# Arguments

height	an acomp, rcomp, aplus, or rplus object giving amounts to be displayed by a barplot
	further graphical parameters as in <b>barplot</b>
legend.text	same as legend.text in barplot
beside	same as beside in <b>barplot</b>
total	The total to be used in displaying the composition, typically 1, 100 or the number of parts

# Details

The functions are essentially light weighted warpers for **barplot** just adding a adequate default behavior for each of the scales.

# Value

A numeric vector (or matrix, when **beside = TRUE**) giving the coordinates of all the bar midpoints drawn, as in **barchart** 

# See Also

acomp, rcomp, rplus aplus, plot.acomp, boxplot.acomp

```
data(SimulatedAmounts)
barplot(mean(acomp(sa.lognormals[1:10,])))
barplot(mean(rcomp(sa.lognormals[1:10,])))
barplot(mean(aplus(sa.lognormals[1:10,])))
barplot(mean(rplus(sa.lognormals[1:10,])))
barplot(acomp(sa.lognormals[1:10,]))
barplot(rcomp(sa.lognormals[1:10,]))
barplot(aplus(sa.lognormals[1:10,]))
barplot(rplus(sa.lognormals[1:10,]))
```

princomp.rplus Principal component analysis for real amounts

# Description

A principal component analysis is done in real geometry (i.e. using iit-transform).

## Usage

```
## S3 method for class 'rplus':
princomp(x,...,scores=TRUE)
## S3 method for class 'princomp.rplus':
print(x,...)
## S3 method for class 'princomp.rplus':
plot(x,y=NULL,...,
npcs=min(10,length(x$sdev)),
type=c("screeplot","variance","biplot","loadings","relative"),
main=NULL,
scale.sdev=1)
## S3 method for class 'princomp.rplus':
predict(object,newdata,...)
```

### Arguments

x	an rplus-dataset (for princomp) or a result from princomp.rplus
У	not used
scores	a logical indicating whether scores should be computed or not
npcs	the number of components to be drawn in the scree plot
type	type of the plot: "screeplot" is a lined screeplot, "variance" is a box- plot like the screeplot, "biplot" is a biplot, "loadings" displays the loadings as a barplot
scale.sdev	the multiple of sigma to use plotting the loadings
main	headline of the plot

object	a fitted princomp.rplus object
newdata	another amount dataset of class rcomp
	further arguments to pass to internally-called functions

## Details

Mainly a princomp(iit(x)) is performed.

The plot routine provides screeplots (type = "s",type= "v"), biplots (type = "b"), plots of the effect of loadings (type = "b") in scale.sdev\*sdev-spread, and loadings of pairwise differences (type = "r").

The interpretation of a screeplot does not differ from ordinary screeplots. It shows the eigenvalues of the covariance matrix, which represent the portions of variance explained by the principal components.

The interpretation of the these biplot uses additionally to the classical interpretation biplots a compositional concept: The differences between two arrowheads can be interpreted as the shift of mass between the two components represented by the arrows.

The amount loading plot is more or less a standard loadings plot. The loadings are displayed by a barplot as positive and negative changes of amounts.

The loadings plot can work in two different modes: If scale.sdev is set to NA it displays the amount vector being represented by the unit vector of loadings in the iit-transformed space. If scale.sdev is numeric we use this amount vector scaled by the standard deviation of the respective component.

The relative plot displays the **relativeLoadings** as a barplot. The deviation from a unit bar shows the effect of each principal component on the respective differences.

## Value

princomp gives an object of type c("princomp.rcomp", "princomp") with the following content:

sdev	the standard deviation of the principal components
loadings	the matrix of variable loadings (i.e., a matrix which columns contain the eigenvectors). This is of class <code>"loadings"</code>
Loadings	The loadings as an "rmult"-object
center	the iit-transformed vector of means used to center the dataset
Center	the <b>rplus</b> vector of means used to center the dataset
scale	the scaling applied to each variable
n.obs	number of observations
scores	if <b>scores = TRUE</b> , the scores of the supplied data on the principal components and the information available. Scores are coordinates in a basis given by the principal components and thus not compositions
call	the matched call
na.action	not clearly understood

predict returns a matrix of scores of the observations in the newdata dataset.

. The other routines are mainly called for their side effect of plotting or printing and return the object  $\mathbf{x}.$
#### See Also

iit,rplus, relativeLoadings princomp.rcomp, princomp.aplus,

#### Examples

```
data(SimulatedAmounts)
pc <- princomp(rplus(sa.lognormals5))</pre>
рс
summary(pc)
plot(pc)
                   #plot(pc,type="screeplot")
plot(pc,type="v")
plot(pc,type="biplot")
plot(pc,choice=c(1,3),type="biplot")
plot(pc,type="loadings")
plot(pc,type="loadings",scale.sdev=-1) # Downward
plot(pc,type="relative",scale.sdev=NA) # The directions
plot(pc,type="relative",scale.sdev=1) # one sigma Upward
plot(pc,type="relative",scale.sdev=-1) # one sigma Downward
biplot(pc)
screeplot(pc)
loadings(pc)
relativeLoadings(pc,mult=FALSE)
relativeLoadings(pc)
relativeLoadings(pc,scale.sdev=1)
relativeLoadings(pc,scale.sdev=2)
pc$sdev^2
cov(predict(pc,sa.lognormals5))
```

gsi.expandrcomp Internal function: Scaling rcomp

# Description

This functions tries to compute something similar to a scaling of an acomp object in the context of the rcomp-geometry.

# Usage

```
gsi.expandrcomp(x,alpha)
```

#### Arguments

х	an rcomp object
alpha	a number or a numeric vector between $0$ and $1$

#### Value

an rcomp-object

## Note

It is better not to use gsi.\* functions directly since they are internal functions of the package

#### Examples

gsi.expandrcomp(rcomp(1:3),0.5)

acomparith

Power transform in Aitchisons simplex

#### Description

The Aitchison Simplex with its two operations perturbation as + and power transform as \* is a vector space. This vector space is represented by these operations.

# Usage

```
power.acomp(x,s)
## Methods for class "acomp"
## x*y
## x/y
```

# Arguments

x	an acomp composition or dataset of compositions (or a number or a numeric vector)
У	a numeric vector of size 1 or $nrow(x)$
S	a numeric vector of size 1 or $nrow(x)$

# Details

The power transform is the basic multiplication operation of the Aitchison simplex seen as a vector space. It is defined as:

$$(x * y)_i := clo((x_i^{y_i})_i)_i$$

The division operation is just the multiplication with 1/y.

# Value

An "acomp" vector or matrix.

# Note

For \* the arguments x and y can be exchanged. Note that this definition generalizes the power by a scalar, since y or s may be given as a scalar, or as a vector with as many components as the composition in acomp x. The result is then a matrix where each row corresponds to the composition powered by one of the scalars in the vector.

#### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

http://ima.udg.es/Activitats/CoDaWork03

http://ima.udg.es/Activitats/CoDaWork05

# See Also

ilr,clr, alr,

#### Examples

```
acomp(1:5)* -1 + acomp(1:5)
data(SimulatedAmounts)
cdata <- acomp(sa.lognormals)
plot( tmp <- (cdata-mean(cdata))/msd(cdata) )
class(tmp)
mean(tmp)
msd(tmp)
var(tmp)</pre>
```

scale

Normalizing datasets by centering and scaling

## Description

The dataset is standardized by optional scaling and centering.

#### Usage

```
## S3 method for class 'acomp':
scale(x,center=TRUE, scale=TRUE)
## S3 method for class 'rcomp':
scale(x,center=TRUE, scale=TRUE)
## S3 method for class 'aplus':
scale(x,center=TRUE, scale=TRUE)
## S3 method for class 'rplus':
```

```
scale(x,center=TRUE, scale=TRUE)
## S3 method for class 'rmult':
scale(x,center=TRUE, scale=TRUE)
```

### Arguments

х	a dataset or a single vector of some type
center	logical value
scale	logical value

# Details

scaling is defined in various ways for the different data types. It is always performed as an operation in the enclosing vector space. Not in all cases an independent scaling of the different coordinates is appropriate. This is only done for rplus and rmult.

#### Value

a vector or data matrix, as x and with the same class, but acordingly transformed.

#### See Also

split{base}

## Examples

```
data(SimulatedAmounts)
plot(scale(acomp(sa.groups)))
## Not run:
plot(scale(rcomp(sa.groups)))
## End(Not run)
plot(scale(aplus(sa.groups)))
## Not run:
plot(scale(rplus(sa.groups)))
## End(Not run)
plot(scale(rmult(sa.groups)))
```

rplusarithm

Arithmetik of rplus-scale

# Description

The positive quadrant forms a manifold of the real vector space. The induced operations +,-,\*,/ give results valued in this real vector space (not necessarily inside the manifold).

#### Usage

```
mul.rplus(x,r)
## Methods for class rplus
## x+y
## x-y
## -x
## -x
## x*r
## r*x
## r*x
## x/r
```

### Arguments

x	an rplus composition or dataset of compositions
У	an rplus composition or dataset of compositions
r	a numeric vector of size 1 or $nrow(x)$

# Details

The functions behave quite like +.rmult.

#### Value

**rmult**-objects containing the given operations on the rcomp manifold as subset of the  $R^D$ . Only the addition and multiplication with positive numbers are internal operation and results in an **rplus**-object again.

# Note

For \* the arguments x and y can be exchanged.

# See Also

+.rmult, +.acomp,cpt, rcomp, rmult

```
rplus(1:5)* -1 + rplus(1:5)
data(SimulatedAmounts)
cdata <- rplus(sa.lognormals)
plot( tmp <- (cdata-mean(cdata))/msd(cdata) )
class(tmp)
mean(tmp)
msd(tmp)
var(tmp)</pre>
```

rplus

## Description

A class to analyse positive amounts in a classical (non-logarithmic) framework.

### Usage

rplus(X,parts=1:NCOL(oneOrDataset(X)),total=NA)

### Arguments

Х	vector or dataset of positive numbers considered as amounts
parts	vector containing the indices xor names of the columns to be used
total	a numeric vectors giving the total amount of each dataset.

## Details

Many multivariate datasets essentially describe amounts of D different parts in a whole. When the whole is large in relation to the considered parts, such that they do not exclude each other, and when the total amount of each componenten is actually determined by the phenomenon under investigation and not by sampling artifacts (such as dilution or sample preparation) then the parts can be treated as amounts rather than as a composition (cf. rcomp, aplus).

In principle, amounts are just real-scaled numbers with the single restriction that they are nonnegative. Thus they can be analysed by any multivariate analysis method. This class provides a simple access interface to do so. It tries to keep in mind the positivity property of amounts and the special point zero. However there are strong arguments why an analyis based on log-scale might be much more adapted to the problem. This log-approach is provided by the class aplus.

The classes rcomp, acomp, aplus, and rplus are designed in a fashion as similar as possible in order to allow direct comparison between results obtained by the different approaches. In particular, the aplus logistic transform **ilt** is mirrored by the simple identity transform **iit**. In terms of computer science, this identity mapping is actually mapping an object of type "rplus" to a class-less datamatrix.

# Value

a vector of class "rplus" representing a vector of amounts or a matrix of class "rplus" representing multiple vectors of amounts, by rows.

#### References

#### See Also

```
iit,rcomp, aplus, princomp.rplus, plot.rplus, boxplot.rplus, barplot.rplus, mean.rplus,
var.rplus, variation.rplus, cov.rplus, msd
```

#### Examples

```
data(SimulatedAmounts)
plot(rplus(sa.lognormals))
```

acompscalarproduct inner product for datasets with a vector space structure

### Description

acomp and aplus objects are considered as (sets of) vectors. The %% is considered as the inner multiplication. An inner multiplication with another vector is the scalar product. An inner multiplication with a matrix is a matrix multiplication, where the vectors are either considered as row or as column vector.

#### Arguments

x %*% y x %*% A A %*% x x %*% y x %*% A A %*% x	
х	a acomp or aplus object
У	a acomp or aplus object
А	a matrix interpreted in clr, ilr or ilt coordinates

# Details

The operators try to mimic the behavior of %%% on c()-vectors as inner product, applied in parallel to all row-vectors of the dataset. Thus the product of a vector with a vector of the same type results in the scalar product of both. For the multiplication with a matrix each vector is considered as a row or column, whatever is more appropriate. The matrix itself is considered as representing a linear mapping (endomorphism) of the vector space to a space of the same type. The mapping is represented in clr, ilr or ilt coordinates. Which of the aforementioned coordinate systems is used is judged from the type of x and from the dimensions of the A.

# Value

Either a numeric vector containing the scalar products, or an object of type acomp or aplus containing the vectors transformed with the given matrix.

# See Also

%\*%.rmult

## Examples

```
x <- acomp(matrix( sqrt(1:12), ncol= 3 ))</pre>
x%*%x
A <- matrix( 1:9,nrow=3)
x %*% A %*% x
x %*% A
A %*% x
A <- matrix( 1:4,nrow=2)
x %*% A %*% x
x %*% A
A %*% x
x <- aplus(matrix( sqrt(1:12), ncol= 3 ))</pre>
x%*%x
A <- matrix( 1:9,nrow=3)
x %*% A %*% x
x %*% A
A %*% x
```

gsi.isSingleRow	Internal function:	Can something	be considered	as a single mul-
	tivariate data iten	n?		

# Description

Checks wether something can be regarded as a single multivariate item, being a matrix or a vector, which is only a row or a column.

### Usage

```
gsi.isSingleRow(X)
```

#### Arguments

the matrix or vector to be checked

# Details

Х

```
It is defined as gsi.isSingleRow <- function(X) { return( NROW(X) == 1 || NCOL(X)
==1 ) }</pre>
```

# Value

a logical value

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

# See Also

gsi

# Examples

gsi.isSingleRow(1:10)

summary.rcomp Summary of compositions in real geometry

# Description

Compute a summary of a composition based on real geometry.

# Usage

## S3 method for class 'rcomp':
summary( object, ... )

# Arguments

object	an <b>rcomp</b> dataset of compositions
	further arguments to summary

# Details

The data is applied a **clo** operation before the computation.

# Value

A matrix containing summary statistics. The value is the same as for the classical summary summary applied to a closed dataset.

# See Also

rcomp, summary.aplus, summary.acomp

# Examples

```
data(SimulatedAmounts)
summary(rcomp(sa.lognormals))
```

plot.aplus

Displaying amounts in scatterplots

# Description

## Usage

```
## S3 method for class 'aplus':
plot(x,...,labels=colnames(X),cn=colnames(X),aspanel=FALSE,id=FALSE,idlabs=NULL,idcol=2,center=
## S3 method for class 'rplus':
plot(x,...,labels=colnames(X),cn=colnames(X),aspanel=FALSE,id=FALSE,idlabs=NULL,idcol=2,center=
## S3 method for class 'rmult':
plot(x,...,labels=colnames(X),cn=colnames(X),aspanel=FALSE,id=FALSE,idlabs=NULL,idcol=2,center=
```

# Arguments

х	a dataset of an amount class
	further graphical parameters passed (see par)
add	a logical indicating whether the information should just be added to an existing plot. In case of false a new plot is created.
col	The color to plot the data.
labels	The names of the parts
cn	The names of the parts to be used in a single panel. Internal use only.
aspanel	Logical indicating that only a single panel should be drawn and not the whole plot. Internal use only.
id	A logical. If true one can identify the points like with the identify command.
idlabs	A character vector providing the labels to be used with the identification, when $\mathtt{id}\texttt{=}TRUE$
idcol	color of the idlabs-labels
center	a logical indicating whether a the data should be centered prior to the plot. Centering is done in the choosen philosophy. See scale
scale	a logical indicating whether a the data should be scaled prior to the plot. Scaling is done in the choosen philosophy. See <pre>scale</pre>

pca	A logical indicating whether the first principle component should be dis- played in the plot. Currently direction of the principle component of the displayed subcomposition is displayed as a line. Later on a the principle
	component of the whole dataset should be displayed.
col.pca	The color to draw the principle component.
logscale	logical indication, whether logscale should be used
xlim	2xncol(x)-matrix giving the xlims for the columns of x
ylim	2xncol(x)-matrix giving the ylims for the columns of x

# Details

TO DO: fix pca bug

# See Also

plot.aplus, qqnorm.acomp,boxplot.acomp

# Examples

```
data(SimulatedAmounts)
plot(aplus(sa.lognormals))
plot(rplus(sa.lognormals))
plot(aplus(sa.lognormals5))
plot(rplus(sa.lognormals5))
```

gsi.diagExtract Internal functions: Get the diagonal of a matrix

# Description

Get the main diagonal of a matrix, even if the matrix is 1x1.

# Usage

gsi.diagExtract(x)

# Arguments

a matrix

# Details

x

The difference to original diag is that it always gives the diagonal and does nothing flawed in case of a 1x1 matrix or a single number considered as such matrix.

# Value

a vector containing the main diagonal entries of x.

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi.diagGenerate, diag

## Examples

```
data(SimulatedAmounts)
gsi.diagExtract(var(acomp(sa.lognormals,c(1,2))))
gsi.diagExtract(var(ilr(acomp(sa.lognormals,c(1,2))))
gsi.diagExtract(var(ilt(aplus(sa.lognormals,c(1))))
```

acompmargin Marginal compositions in Aitchison Compositions

## Description

Compute marginal compositions of selected parts, by computing the rest as the geometric mean of the non-selected parts.

# Usage

```
acompmargin(X,d=c(1,2),name="*",pos=length(d)+1)
```

# Arguments

Х	composition or dataset of compositions
d	vector containing the indices xor names of the columns selected
name	The new name of the amalgamation column
pos	The position where the new amalgamation column should be stored. This defaults to the last column.

# Details

The amalgamation column is simply computed by taking the geometric mean of the nonselected components. This is consistent with the **acomp** approach and gives clear ternary diagrams. However, this geometric mean is difficult to interpret.

#### Value

A closed compositions with class "acomp" containing the variables given by d and the the amalgamation column.

#### References

Vera Pawlowsky-Glahn (2003) personal communication. Seminaris d'Estadística, Departament d'Informàtica i Matemàtica Aplicada, Universitat de Girona.

## See Also

rcompmargin, acomp

## Examples

```
data(SimulatedAmounts)
plot.acomp(sa.lognormals5,margin="acomp")
plot.acomp(acompmargin(sa.lognormals5,c("Pb","Zn")))
plot.acomp(acompmargin(sa.lognormals5,c(1,2)))
```

```
rnorm
```

Normal distributions on special spaces

#### Description

rnorm. X generates multivariate normal random variates in the space X.

#### Usage

```
rnorm.acomp(n,mean,var)
rnorm.rcomp(n,mean,var)
rnorm.aplus(n,mean,var)
rnorm.rplus(n,mean,var)
rnorm.rmult(n,mean,var)
dnorm.acomp(x,mean,var)
dnorm.aplus(x,mean,var)
dnorm.rmult(x,mean,var)
```

#### Arguments

n	number of datasets to be simulated
mean	The mean of the dataset to be simulated
var	The variance covariance matrix
x	vectors in the sampling space

#### Details

The normal distributions in the variouse spaces dramatically differ. The normal distribution in the **rmult** space is the commonly known multivariate joint normal distribution. For **rplus** this distribution has to be somehow truncated at 0. This is here done by setting negative values to 0.

The normal distribution of **rcomp** is seen as a normal distribution within the simplex as a geometrical portion of the real vector space. The variance is thus forced to be singular and restricted to the affine subspace generated by the simplex. The necessary truncation of negative values is currently done by setting them explicitly to zero and reclosing afterwards. The **"acomp"** and **"aplus"** are itself metric vector spaces and thus a normal distribution is defined in them just as in the real space. The resulting distribution corresponds to a multivariate lognormal in the case of **"aplus"** and in Aitchisons normal distribution in the simplex in the case of **"acomp"** (TO DO: Is that right??).

For the vector spaces **rmult**, **aplus**, **acomp** it is further possible to provide densities with repect to their Lebesgue measure. In the other cases this is not possible since the resulting distributions are not absolutly continues with respect to such a measure due to the truncation.

#### Value

a random dataset of the given class generated by a normal distribution with the given mean and variance in the given space.

## References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

### See Also

runif.acomp, rlnorm.rplus, rDirichlet.acomp

## Examples

```
MyVar <- matrix(c(
0.2,0.1,0.0,
0.1,0.2,0.0,
0.0,0.0,0.2),byrow=TRUE,nrow=3)
MyMean <- c(1,1,2)</pre>
```

plot(rnorm.acomp(100,MyMean,MyVar))

```
plot(rnorm.rcomp(100,MyMean,MyVar))
plot(rnorm.aplus(100,MyMean,MyVar))
plot(rnorm.rplus(100,MyMean,MyVar))
plot(rnorm.rmult(100,MyMean,MyVar))
x <- rnorm.aplus(5,MyMean,MyVar)
dnorm.acomp(x,MyMean,MyVar)
dnorm.aplus(x,MyMean,MyVar)
dnorm.rmult(x,MyMean,MyVar)</pre>
```

normalize

Normalize vectors to norm 1

# Description

Normalize vectors to norm 1.

# Usage

normalize(x,...)
## Default S3 method:
normalize(x,...)

## Arguments

х	a dataset or a single vector of some type							
	currently not used, intended to select a different norm							

# Value

The vectors given, but normalized to norm 1.

## See Also

norm

```
data(SimulatedAmounts)
normalize(c(1,2,3))
normalize(acomp(c(1,2,3)))
norm(normalize(acomp(sa.groups)))
```

is.acomp

# Description

is.XXX returns TRUE if and only if its argument is of type XXX

# Usage

is.acomp(x)
is.rcomp(x)
is.aplus(x)
is.rplus(x)
is.rmult(x)

# Arguments

x any object to be checked

### Details

These functions only check for the class of the object.

# Value

TRUE or FALSE

# See Also

acomp, rcomp aplus, rplus

```
is.acomp(1:3)
is.acomp(acomp(1:3))
is.rcomp(acomp(1:3))
is.acomp(acomp(1:3)+acomp(1:3))
```

runif

## Description

Generates random compositions with a uniform distribution on the (rcomp) simplex.

#### Usage

```
runif.acomp(n,D)
runif.rcomp(n,D)
```

#### Arguments

n	number of datasets to be simulated
D	number of parts

# Value

a generated random dataset of class "acomp" or "rcomp" with drawn from a uniform distribution on the simplex of D parts.

## Note

The only difference between both routines is the type of the returned dataset.

# References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

# See Also

rDirichlet.acomp

```
plot(runif.acomp(10,3))
plot(runif.rcomp(10,3))
```

rmultmatmult

#### Description

An rmult object is considered as a sequence of vectors. The %\*% is considered as the inner multiplication. An inner multiplication with another vector is the scalar product. an inner multiplication with a matrix is a matrix multiplication, where the rmult-vectors are either considered as row or as column vector.

#### Arguments

x %\*% y x %\*% v v %\*% x x %\*% A A %\*% x w %\*% A A %\*% w w %\*% x x %\*% w x an rmult vector or dataset of vectors y an rmult vector or dataset of vectors

У	an rmult vector or dataset of vectors
v	a numeric vector of length gsi.getD(x)
W	a numeric vector of length gsi.getD(x)
А	a matrix

# Details

The operators try to minic the behavior of %% on c()-vectors as inner product applied in parallel to all vectors of the dataset. Thus the product of a vector with another **rmult** object or unclassed vector v results in the scalar product. For the multiplication with a matrix each vector is considered as a row or column, whatever is more appropriate.

# Value

an object of class "rmult" or a numeric vector containing the result of the corresponding inner products.

# Note

The product x %\*% A %\*% y is associative.

## See Also

rmult, %\*%.rmult

#### Examples

```
x <- rmult(matrix( sqrt(1:12), ncol= 3 ))
x%*%x
A <- matrix( 1:9,nrow=3)
x %*% A %*% x
x %*% A
A %*% x
x %*% 1:3
x %*% 1:3
1:3 %*% x</pre>
```

```
gsipairs
```

Internal functions of the compositions package

# Description

Creates a paired plot like pairs but allows to add additional panels afterwards

#### Usage

```
gsi.pairs(x, labels, panel = points, ..., main = NULL, oma = NULL,
font.main = par("font.main"), cex.main = par("cex.main"),
lower.panel = panel, upper.panel = panel, diag.panel = NULL,
text.panel = textPanel, label.pos = 0.5 + has.diag/3, cex.labels = NULL,
font.labels = 1, row1attop = TRUE, gap = 1,add=list(),xlim=apply(x,2,range),ylim=apply(x,2,
gsi.add2pairs(x,panel,...,noplot=FALSE)
gsi.plots
```

### Arguments

x	a multivariate dataset						
labels	The names of the variables						
panel	The function to perform the actual pairwise plots.						
	see pairs						
main	see pairs						
oma	see pairs						
font.main	see pairs						
cex.main	see pairs						
lower.panel	see pairs						
upper.panel	see pairs						
diag.panel	see pairs						
text.panel	see pairs						
label.pos	see pairs						

cex.labels	see pairs
font.labels	see pairs
row1attop	see pairs
gap	see pairs
add	additional parameter containing a list of additional panels
xlim	additional $2xncol(x)$ -matrix parameter giving in $xlim[,j]$ the xlims of the j-th column
ylim	additional $2xncol(x)$ -matrix parameter giving in ylim[,i] the ylims of the j-th column
log	additional parameter with possible values like in $\verb"plot"$ allowing to log some plots, without a warning
noplot	Logical indicating wether the plotting should be suppressed. This is usefull for plotting single page postscripts.

## Details

gsi.pairs essentially copies the functionality of pairs. However it additionally stores its own parameters in the dev.cur() position of gsi.plots and allows to modify the parameters and redo a modified plot afterwards. This is mainly done by gsi.add2pairs by modifying the additional add parameter, that specifies more panels. This meachnism showed not be used directly since it is planed to replace the whole meachnism by a more rigor solution soon.

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

gsi,

# Examples

perturbe

Perturbation of compositions

# Description

The perturbation is the addition operation in the Aitchison geometry of the simplex.

Usage

```
perturbe(x,y)
## Methods for class "acomp"
## x + y
## x - y
## - x
```

### Arguments

х	$\operatorname{compositions}$	of	class	acomp
У	$\operatorname{compositions}$	of	class	acomp

# Details

The perturbation is the basic addition operation of the Aitichson simplex as a vector space. It is defined by:

$$(x+y)_i = clo((x_iy_i)_i)_i$$

permute and + compute this operation. The only difference is that + checks the class of its argument, while permute does not check the type of the arguments and can thus directly be applied to a composition in any form (unclassed, acomp, rcomp).

The - operation is the inverse of the addition in the usual way and defined by:

$$(x-y)_i := clo((x_i/y_i)_i)_i$$

and as unary operation respectively as:

$$(-x)_i := clo((1/y_i)_i)_i$$

# Value

An acomp vector or matrix.

## References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

# See Also

acomp, \*.aplus, +.rplus

```
tmp <- -acomp(1:3)
tmp + acomp(1:3)</pre>
```

variation

#### Description

Compute the variation matrix in the various approaches of compositional and amount data analysis. Pay attention that this is not computing the variance or covariance matrix!

#### Usage

```
variation(x,...)
## S3 method for class 'acomp':
variation(x, ...)
## S3 method for class 'rcomp':
variation(x, ...)
## S3 method for class 'aplus':
variation(x, ...)
## S3 method for class 'rplus':
variation(x, ...)
## S3 method for class 'rmult':
variation(x, ...)
```

## Arguments

x	a dataset, eventually of amounts or compositions
	currently unused

## Details

The variation matrix was defined in the acomp context for analysis of compositions as the matrix of variances of all possible log-ratios among components (Aitchison, 1986). The generalization to rcomp objects is simply to reproduce the variance of all possible differences between components. The amount and rmult objects should not be treated with variation matrices, because this implies always the existence of a closure.

# Value

The variation matrix of x.

## See Also

cdt, clrvar2ilr, clo, mean.acomp, acomp, rcomp, aplus, rplus

#### Examples

```
data(SimulatedAmounts)
mean.col(sa.lognormals)
variation(acomp(sa.lognormals))
variation(rcomp(sa.lognormals))
variation(aplus(sa.lognormals))
variation(rplus(sa.lognormals))
variation(rmult(sa.lognormals))
```

ult

#### Uncentered log transform

# Description

Compute the uncentered log ratio transform of a (dataset of) composition(s) and its inverse.

### Usage

ult( x )
ult.inv( z )
Kappa( x )

# Arguments

х	a composition or a data matrix of compositions, not necessarily closed
Z	the ult-transform of a composition or a data matrix of clr-transforms of
	compositions, not necessarily centered

# Details

The ult-transform is simply the elementwise log of the closed composition. The ult has some important properties in the scope of Information Theory.

### Value

ult gives the uncentered log transform, ult.inv gives closed compositions with the given ult-transforms Kappa gives the difference between the clr and the ult transform. It is quite linked to information measures.

# See Also

ilr,alr,apt

#### Examples

```
(tmp <- ult(c(1,2,3)))
ult.inv(tmp)
ult.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(ult(cdata))
Kappa(c(1,2,3))</pre>
```

```
qqnorm
```

Normal quantile plots for compositions and amounts

# Description

The plots allow to check the normal distribution of multiple univaritate marginals by normal-quantile-quantile plots. For the different interpretations of amount data a different type of normality is assumed and checked. When an alpha-level is given the marginal displayed in each panel is checked for normality.

### Usage

```
## S3 method for class 'acomp':
qqnorm(y,fak=NULL,...,panel=vp.qqnorm,alpha=NULL)
## S3 method for class 'rcomp':
qqnorm(y,fak=NULL,...,panel=vp.qqnorm,alpha=NULL)
## S3 method for class 'aplus':
qqnorm(y,fak=NULL,...,panel=vp.qqnorm,alpha=NULL)
## S3 method for class 'rplus':
qqnorm(y,fak=NULL,...,panel=vp.qqnorm,alpha=NULL)
vp.qqnorm(x,y,...,alpha=NULL)
```

#### Arguments

У	a dataset
fak	a factor to split the dataset, not yet implemented in aplus and rplus
panel	the panel function to be used or a list of multiple panel functions
alpha	The alpha level of a test for normality to be performed for each of the displayed marginals. The levels are adjusted for multiple testing with a Bonferroni-correction (i.e. dividing each of the the alpha-level by the number of test performed)
	further graphical parameters
x	used by pairs only

#### Details

qqnorm.rplus and qqnorm.rcomp displays qqnorm-plots of individual amounts (on the diagonal), of pairwise differences of amounts (above the diagonal) and of pairwise sums of amounts (below the diagonal).

qqnorm.aplus displays qqnorm-plots of individual log-amounts (on the diagonal), of pairwise log-rations of amounts (above the diagonal) and of pairwise sums of log amount (below the diagonal).

qqnorm.aplus displays qqnorm-plots of pairwise log-ratios of amounts in all of diagonal panels. Nothing is displayed on the diagonal.

In all cases a joint normality of the original data in the selected framework would imply normality in all displayed marginal distributions.

The marginal normality can be checked in each of the plots using a **shapiro.test**, by specifying an alpha level. The alpha level are corrected for multiple testing. Plots displaying a marginal distribution significantly deviating from a normal distribution are marked by a red exclamation mark.

vp.qqnorm is used as a panel function to make high dimensional plots.

#### See Also

plot.acomp, boxplot.acomp, rnorm.acomp, rnorm.rcomp, rnorm.aplus, rnorm.rplus

# Examples

```
data(SimulatedAmounts)
qqnorm(acomp(sa.lognormals),alpha=0.05)
qqnorm(rcomp(sa.lognormals),alpha=0.05)
qqnorm(aplus(sa.lognormals),alpha=0.05)
qqnorm(rplus(sa.lognormals),alpha=0.05)
```

princomp.aplus Principal component analysis for amounts in log geometry

## Description

A principal component analysis is done in the Aitchison geometry (i.e. ilt-transform). Some gimics simplify the interpretation of the computed components as amount perturbations.

### Usage

```
## S3 method for class 'aplus':
princomp(x,...,scores=TRUE)
## S3 method for class 'princomp.aplus':
print(x,...)
## S3 method for class 'princomp.aplus':
plot(x,y=NULL,...,
npcs=min(10,length(x$sdev)),
type=c("screeplot","variance","biplot","loadings","relative"),
```

```
main=NULL,
scale.sdev=1)
## S3 method for class 'princomp.aplus':
predict(object,newdata,...)
```

#### Arguments

x	an aplus dataset (for princomp) or a result from princomp.aplus
У	not used
scores	a logical indicating whether scores should be computed or not
npcs	the number of components to be drawn in the scree plot
type	type of the plot: "screeplot" is a lined screeplot, "variance" is a boxplot like screeplot, "biplot" is a biplot, "loadings" displayes the Loadings as a barplot.acomp
scale.sdev	the multiple of sigma to use plotting the loadings
main	headline of the plot
object	a fitted princomp.aplus object
newdata	another amount dataset of class aplus
•••	further arguments to pass to internally-called functions

#### Details

As a metric euclidean space, the positive real space described in **aplus** has its own principal component analysis, that should be performed in terms of the covariance matrix and not in terms of the meaningless correlation matrix.

To aid the interpretation we added some extra functionality to a normal princomp(ilt(x)). First of all the result contains as additional information the amount representation of returned vectors in the space of the data: the center as amount Center, and the loadings in terms of amounts to perturbe with positively (Loadings) or negativly (DownLoadings). The Up- and DownLoadings are normalized to the number of parts and not to one to simplify the interpretation. A value of about one means no change in the specific component. The plot routine provides screeplots (type = "s",type= "v"), biplots (type = "b"), plots of the effect of loadings (type = "b") in scale.sdev\*sdev-spread, and loadings of pairwise (log-)ratios (type = "r").

The interpretation of a screeplot does not differ from ordinary screeplots. It shows the eigenvalues of the covariance matrix, which represent the portions of variance explained by the principal components.

The interpretation of the biplot uses additionally to the classical one a compositional concept: The differences between two arrowheads can be interpreted as log-ratios between the two components represented by the arrows.

The amount loading plot is introduced with this package. The loadings of all component can be seen as an orthogonal basis in the space of *ilt*-transformed data. These vectors are displayed by a barplot with their corresponding amounts. A portion of one means no change of this part. This is equivalent to a zero loading in a real principal component analysis.

The loadings plot can work in two different modes: If scale.sdev is set to NA it displays the amount vector being represented by the unit vector of loadings in the ilt-transformed space. If scale.sdev is numeric we use the this amount vector scaled by the standard deviation of the respective component.

The relative plot displays the **relativeLoadings** as a barplot. The deviation from a unit bar shows the effect of each principal component on the respective ratio. The interpretation of the ratios plot may only be done in an Aitchison-compositional framework.

#### Value

princomp gives an object of type c("princomp.acomp", "princomp") with the following content:

sdev	the standard deviation of the principal components
loadings	the matrix of variable loadings (i.e., a matrix which columns contain the eigenvectors). This is of class "loadings".
center	the ilt-transformed vector of means used to center the dataset
Center	the <b>aplus</b> vector of means used to center the dataset
scale	the scaling applied to each variable
n.obs	number of observations
scores	if <b>scores</b> = <b>TRUE</b> , the scores of the supplied data on the principal components and the information available. Scores are coordinates in a basis given by the principal components and thus not compositions
call	the matched call
na.action	not clearly understood
Loadings	vectors of amounts that represent a perturbation with the vectors repre- sented by the loadings of each of the factors
DownLoadings	vectors of amounts that represent a perturbation with the inverses of the vectors represented by the loadings of each of the factors

predict returns a matrix of scores of the observations in the newdata dataset

. The other routines are mainly called for their side effect of plotting or printing and return the object  ${\tt x}.$ 

## See Also

ilt,aplus, relativeLoadings princomp.acomp, princomp.rplus, barplot.aplus, mean.aplus,

```
data(SimulatedAmounts)
pc <- princomp(aplus(sa.lognormals5))
pc
summary(pc)
plot(pc, type="v")
plot(pc,type="v")
plot(pc,choice=c(1,3),type="biplot")
plot(pc,type="loadings")
plot(pc,type="loadings",scale.sdev=-1) # Downward</pre>
```

```
plot(pc,type="relative",scale.sdev=NA) # The directions
plot(pc,type="relative",scale.sdev=1) # one sigma Upward
plot(pc,type="relative",scale.sdev=-1) # one sigma Downward
biplot(pc)
screeplot(pc)
loadings(pc)
relativeLoadings(pc,mult=FALSE)
relativeLoadings(pc,scale.sdev=1)
relativeLoadings(pc,scale.sdev=2)
pc$Loadings
pc$DownLoadings
barplot(pc$Loadings)
```

pc\$sdev^2
cov(predict(pc,sa.lognormals5))

```
scalar
```

Parallel scalar products

# Description

#### Usage

```
scalar(x,y)
## Default S3 method:
scalar(x,y)
```

### Arguments

х	a vector	or a	matrix	with	rows	considered	as	vectors
У	a vector	or a	matrix	with	rows	considered	as	vectors

### Details

The scalar product of two vectors is defined as:

$$scalar(x,y) := \sum (x_i y_i)$$

#### Value

a numerical vector containing the scalar products of the vectors given by x and y. If both x and y contain more than one vector the function uses parallel operation like it would happen with an ordinary product of vectors.

# Note

The computation of the scalar product implicitly applies the cdt transform, which implies that the scalar products corresponding to the given geometries are returned for acomp, rcomp, aplus, rplus-objects. Even a useful scalar product for factors is defined.

## Examples

scalar

oneOrDataset Treating single compositions as one-row datasets

# Description

A dataset is converted to a data matrix. A single data item (i.e. a simple vector) is converted to a one-row data matrix.

# Usage

oneOrDataset(W,B=NULL)

#### Arguments

W	a vector, matrix or dataframe
В	an optional second vector, matrix or data frame having the intended num- ber of rows.

# Value

A data matrix containing the same data as W. If W is a vector it is interpreded as a single row. If B is given and length(dim(B))!= 2 and W is a vector, then W is repeated nrow(B) times.

# See Also

```
oneOrDataset(c(1,2,3))
oneOrDataset(c(1,2,3),matrix(1:12,nrow=4))
oneOrDataset(data.frame(matrix(1:12,nrow=4)))
```

rDirichlet

# Description

The Dirichlet distribution on the simplex.

# Usage

rDirichlet.acomp(n,alpha)
rDirichlet.rcomp(n,alpha)

#### Arguments

n	number of datasets to be simulated
alpha	parameters of the Dirichlet distribution

# Details

TO DO!!!

## Value

a generated random dataset of class "acomp" or "rcomp" with drawn from a Dirichlet distribution with the given parameter alpha. The names of alpha are used to name the parts.

# References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

# See Also

rnorm.acomp

```
tmp <- rDirichlet.acomp(10,alpha=c(A=2,B=0.2,C=0.2))
plot(tmp)</pre>
```

#### Description

A class to analyse positive amounts in a logistic framework.

#### Usage

```
aplus(X,parts=1:NCOL(oneOrDataset(X)),total=NA)
```

#### Arguments

Х	vector or dataset of positive numbers
parts	vector containing the indices xor names of the columns to be used
total	a numeric vectors giving the total amounts of each dataset.

## Details

Many multivariate datasets essentially describe amounts of D different parts in a whole. When the whole is large in relation to the considered parts, such that they do not exclude each other, or when the total amount of each componenten is indeed determined by the phenomenon under investigation and not by sampling artifacts (such as dilution or sample preparation), then the parts can be treated as amounts rather than as a composition (cf. acomp, rcomp).

Like compositions, amounts have some important properties. Amounts are always positive. An amount of exactly zero essentially means that we have a substance of an other quality. Different amounts - spanning different orders of magnitude - are often given in different units (ppm, ppb, %) and conversion factors need not to be fixed (e.g. for ppm, g/l, vol.%, mass %, molar fraction). Often, these amounts are also taken as indicators of other non-measured components (e.g. K as indicator for potassium feldspar), which might be proportional to the measured amount. However, in contrast to compositions, amounts themselves do matter. Amounts are typically heavily skewed and in many practical cases a log-transform makes their distribution roughly symmetric, even normal.

In full analogy to Aitchison's compositions, we introduce vector space operations for amounts: the perturbation perturbe.aplus as a vector space addition (corresponding to change of units), the power transformation power.aplus as scalar multiplication describing the law of mass action, and a distance dist which is independent of the chosen units. The induced vector space is mapped isometrically to a classical  $R^D$  by a simple log-transformation called ilt, resembling classical log transform approaches.

The general approach in analysing aplus objects is thus to perform classical multivariate analysis on ilt-transformed coordinates and to backtransform or display the results in such a way that they can be interpreted in terms of the original amounts.

The class aplus is complemented by the **rplus**, allowing to analyse amounts directly as real numbers, and by the classes **acomp** and **rcomp** to analyse the same data as compositions disregarding the total amounts, focusing on relative amounts only.

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aplus

The classes rcomp, acomp, aplus, and rplus are designed as similar as possible in order to allow direct comparison between results achieved by the different approaches. Especially the acomp simplex transforms clr, alr, ilr are mirrored in the aplus class by the single bijective isometric transform ilt

## Value

a vector of class "aplus" representing a vector of amounts or a matrix of class "aplus" representing multiple vectors of amounts, each vector in one row.

#### References

#### See Also

ilt,acomp, rplus, princomp.aplus, plot.aplus, boxplot.aplus, barplot.aplus, mean.aplus, var.aplus, variation.aplus, cov.aplus, msd

# Examples

```
data(SimulatedAmounts)
plot(aplus(sa.lognormals))
```

gsiinternal Internal functions of the compositions package

## Description

Internal function to compute 2D marginal compositions for plots

#### Usage

```
gsi.plotmargin(X,d,margin)
```

#### Arguments

Х	A multivariate compositional dataset
d	a numeric or character vector of two elements specifying the margin
margin	a character specifying the type of margin to be choosen. Possible values
	are "acomp", "rcomp" or a column name from the dataset.

# Details

#### Value

a composition of three elements.

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi

# Examples

alr

#### Additive log ratio transform

# Description

Compute the additive log ratio transform of a (dataset of) composition(s), and its inverse.

### Usage

alr( x )
alr.inv( z )

#### Arguments

х	a composition, not necessarily closed
z	the alr-transform of a composition, thus a (D-1)-dimensional real vector

## Details

The alr-transform maps a composition in the D-part Aitchison-simplex non-isometrically to a D-1 dimensional euclidian vector, treating the last part as common denominator of the others. The data can then be analysed in this transformation by all classical multivariate analysis tools not relying on a distance. The interpretation of the results is relatively simple, since the relation to the original D-1 first parts is preserved. However distance is an extremely relevant concept in most types of analysis, where a clr or ilr transformation should be preferred.

The additive logratio transform is given by

$$alr(x)_i := \ln \frac{x_i}{x_D}$$

# Value

alr gives the additive log ratio transform; accepts a compositional dataset alr.inv gives a closed composition with the given alr-transform; accepts a dataset

## References

Aitchison, J. (1986) The Statistical Analysis of Compositional Data Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

# See Also

clr,alr,apt, http://ima.udg.es/Activitats/CoDaWork03

## Examples

```
(tmp <- alr(c(1,2,3)))
alr.inv(tmp)
unclass(alr.inv(tmp)) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(alr(cdata))</pre>
```

princomp.rmult Principle component analysis for Real data

#### Description

Performes a principle component analysis for datasets of type rmult.

# Usage

## S3 method for class 'rmult':
princomp(x,...)

### Arguments

х	a rmult-dataset
•••	Further arguments to call of princomp.default

# Details

The function just does  $princomp(unclass(x), \ldots, scale=scale)$  and is only here for convenience.

# Value

An object of type princomp with the following fields

sdev	the standard deviation of the principle components.
loadings	the matrix of variable loadings (i.e., a matrix whose columns contain the eigenvectors). This is of class "loadings". The last eigenspace is removed since it should contain the irrelevant scaling.
center	the clr of the means that was substracted

scale	the scaling applied to each variable
n.obs	number of observations
scores	if <b>scores = TRUE</b> , the scores of the supplied data on the principle components and the information was available. Scores are coordinates in a basis given by the principle components and thus not compositions.
call	the matched call
na.action	Not clearly understood

# See Also

princomp.rplus

# Examples

```
data(SimulatedAmounts)
pc <- princomp(rmult(sa.lognormals5))
pc
summary(pc)
plot(pc)
screeplot(pc,type="l")
biplot(pc,choice=c(1,3))
loadings(pc)
plot(loadings(pc))
pc$sdev^2
cov(predict(pc,sa.lognormals5))</pre>
```

totals

Total sum of amounts

# Description

Calculates the total amount by summing the individual parts.

# Usage

```
totals(x,...)
## S3 method for class 'acomp':
totals(x,...)
## S3 method for class 'rcomp':
totals(x,...)
## S3 method for class 'aplus':
totals(x,...)
## S3 method for class 'rplus':
totals(x,...)
```

#### Arguments

х	an amount/amount dataset
	not used, only here for generics

# Value

a numeric vector containing the total amounts

### See Also

aplus

# Examples

```
data(SimulatedAmounts)
totals(acomp(sa.lognormals))
totals(rcomp(sa.lognormals,total=100))
totals(aplus(sa.lognormals))
totals(rplus(sa.lognormals))
aplus(acomp(sa.lognormals),total=totals(aplus(sa.lognormals)))
```

```
lines
```

Draws connected lines from point to point.

#### Description

Functions taking coordinates given in various ways and joining the corresponding points with line segments.

## Usage

```
## S3 method for class 'acomp':
lines(x,...,steps=30)
## S3 method for class 'rcomp':
lines(x,...,steps=30)
## S3 method for class 'aplus':
lines(x,...,steps=30)
## S3 method for class 'rplus':
lines(x,...,steps=30)
## S3 method for class 'rmult':
lines(x,...,steps=30)
```

# Arguments

х	a dataset of the given type
	further graphical parameters
steps	the numer of discretisation points to draw the segments not straight on
	the monitor.
### Details

The functions add lines to the graphics generated with the corresponding plot functions.

Adding to multipaneled plots, redraws the plot completely and is only possible, when the plot has been created with the plotting routines from this library.

#### See Also

plot.acomp, straight

#### Examples

data(SimulatedAmounts)

```
plot(acomp(sa.lognormals))
lines(acomp(sa.lognormals),col="red")
lines(rcomp(sa.lognormals),col="blue")
plot(aplus(sa.lognormals[,1:2]))
lines(aplus(sa.lognormals[,1:2]),col="red")
lines(rplus(sa.lognormals)[,1:2],col="blue")
plot(rplus(sa.lognormals[,1:2]))
```

```
tt<-aplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="red")
tt<-rplus(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="blue")
tt<-rmult(sa.lognormals[,1:2]); ellipses(mean(tt),var(tt),r=2,col="green")</pre>
```

summary.acomp Summarizing a compositional dataset in terms of ratios

### Description

Summaries in terms of compositions are quite different from classical ones. Instead of analysing each variable individually, we must analyse each pairwise ratio in a log geometry.

## Usage

## S3 method for class 'acomp': summary( object, ... )

## Arguments

object	a data.matrix of compositions, not necessarily closed
	not used, only here for generics

## Details

It is quite difficult to summarize a composition in a consistent and interpretable way. We tried to provide such a summary here.

# Value

The result is an object of type "summary.acomp"

mean	The mean.acomp composition
mean.ratio	A matrix containing the geometric mean of the pairwise ratios
variation	The variation matrix of the dataset ({variation.acomp})
expsd	A matrix containing the one-sigma factor for each ratio, computed as exp(sqrt(variation.acomp(W))). To obtain two-sigma-factor it needs to be squared. To obtain the reverse bound we compute 1/expsd
min	A matrix containing the minimum of each of the pairwise ratios
q1	A matrix containing the 1-Quartile of each of the pairwise ratios
median	A matrix containing the median of each of the pairwise ratios
q1	A matrix containing the 3-Quartile of each of the pairwise ratios
max	A matrix containing the maximum of each of the pairwise ratios

#### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

#### See Also

## acomp

## Examples

```
data(SimulatedAmounts)
summary(acomp(sa.lognormals))
```

rmult

 $Simple\ treatment\ of\ real\ vectors$ 

## Description

A class to analyse real multivariate vectors.

### Usage

rmult(X,parts=1:NCOL(oneOrDataset(X)))

#### Arguments

Х	vector or dataset of numbers considered as elements of a R-vector
parts	vector containing the indices xor names of the columns to be used

#### Details

The **rmult** class is a simple convenience class to treat data in the scale of real vectors just like data in the scale of real numbers. A major aspect to take into account is that the internal arithmetic of R is different for these vectors.

## Value

a vector of class "rmult" representing one vector or a matrix of class "rmult", representing multiple vectors by rows.

## See Also

+.rmult, scalar, norm, %\*%.rmult, rplus, acomp,

## Examples

```
plot(rnorm.rmult(30,mean=0:4,var=diag(1:5)+10))
```

gsi.eps

Internal variable: Negligible differences

## Description

fixes or yields the internal value for differences to be considered as zero.

#### Usage

gsi.eps

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

gsi

#### Description

Compute the additive planar transform of a (dataset of) compositions and its inverse.

### Usage

apt( x )
apt.inv( z )

### Arguments

x	a composition or a matrix of compositions, not necessarily closed
Z	the apt-transform of a composition or a matrix of alr-transforms of com-
	positions

# Details

The apt-transform maps a composition in the D-part real-simplex linearly to a D-1 dimensional euclidian vector. Although the transformation does not reach the whole  $R^{D-1}$ , resulting covariance matrices are typically of full rank.

The data can then be analysed in this transformation by all classical multivariate analysis tools not relying on distances. See cpt and ipt for alternatives. The interpretation of the results is easy since the relation to the first D-1 original variables is preserved.

The additive planar transform is given by

$$apt(x)_i := clo(x)_i, i = 1, \dots, D-1$$

## Value

apt gives the centered planar transform, apt.inv gives closed compositions with the given apt-transforms

### References

## See Also

alr,cpt,ipt

apt

#### Examples

```
(tmp <- apt(c(1,2,3)))
apt.inv(tmp)
apt.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(apt(cdata))</pre>
```

### idt

Isometric default transform

### Description

Compute the isometric default transform of a vector (or dataset) of compositions or amounts in the selected class.

### Usage

```
idt(x)
## Default S3 method:
idt( x )
## S3 method for class 'acomp':
idt( x )
## S3 method for class 'rcomp':
idt( x )
## S3 method for class 'aplus':
idt( x )
## S3 method for class 'rplus':
idt( x )
## S3 method for class 'rmult':
idt( x )
## S3 method for class 'factor':
idt( x )
```

#### Arguments

х

a classed amount or composition, to be transformed with its isometric default transform

#### Details

The general idea of this package is to analyse the same data with different geometric concepts, in a fashion as similar as possible. For each of the four concepts there exists an isometric transform expressing the geometry in a full-rank euclidean vector space. Such a transformation is computed by idt. For acomp the transform is ilr, for rcomp it is ipt, for aplus it is ilt, and for rplus it is iit. Keep in mind that the transform does not keep the variable names, since there is no guaranteed one-to-one relation between the original parts and each transformed variable.

#### Value

A corresponding matrix of row-vectors containing the transforms.

### References

See Also

cdt, ilr, ipt, ilt, iit

### Examples

```
## Not run:
# the idt is defined by
idt <- function(x) UseMethod("idt",x)
idt.default <- function(x) x
idt.acomp <- function(x) ilr(x)
idt.rcomp <- function(x) ipt(x)
idt.aplus <- ilt
idt.rplus <- iit
## End(Not run)
idt(acomp(1:5))
idt(rcomp(1:5))
```

endpointCoordinates Amounts in barytic-coordinates

## Description

Computes the convex combination of amounts given by endpoints to explain X as good as possible.

## Usage

```
endpointCoordinates(X,...)
endpointCoordinatesInv(K,endpoints,...)
## Default S3 method:
endpointCoordinates(X,endpoints=diag(gsi.getD(X)), ...)
## S3 method for class 'acomp':
endpointCoordinates(X,endpoints=clr.inv(diag(gsi.getD(X))),...)
## S3 method for class 'aplus':
endpointCoordinates(X,endpoints,...)
## S3 method for class 'rplus':
endpointCoordinates(X,endpoints,...)
## S3 method for class 'rmlut':
```

```
endpointCoordinatesInv(K,endpoints,...)
## S3 method for class 'acomp':
endpointCoordinatesInv(K,endpoints,...)
## S3 method for class 'rcomp':
endpointCoordinatesInv(K,endpoints,...)
## S3 method for class 'aplus':
endpointCoordinatesInv(K,endpoints,...)
## S3 method for class 'rplus':
endpointCoordinatesInv(K,endpoints,...)
```

#### Arguments

Х	a dataset of amounts or compositions, to be represented in as convex combination of the endpoints in the given geometry
К	Konvex combination weights to the endpoints
endpoints	a dataset of extremal compositions from the same space as X. The number of endpoints given must not exceed the dimension of the space plus one.
	currently unused

#### Details

The convex combination is performed in the respective geometry. This means that for rcomp positivity of the result is only guaranteed with external endmembers and that in acomp-geometry it is not possible to give extremal endmembers.

The main idea behind this functions is that the actually observed composition came from a convex combination of some extremal compositions specified by endpoints. Strictly speaking this is meaningfull in strictly this sense only in rplus-geometry and under some special circumstances in rcomp geometry. It is not meaningfull in terms of mass conservation in acomp- and aplus-geometry due to the non mass-balancing character of the geometry. In rcomp-geometry it dependent on unit of measurements and different for volume and mass % and only valid if the whole composition is observed.

### Value

The endpointCoordinates functions give a "rmult"-dataset giving the convex weights, which allow to combine X from endpoints as good as possible. The result is an "rmult" since there is guarantee that the resulting weights are positive.

The endpointCoordinates functions reconstruct the convex combination from coordinates K and the given endpoints. The class of endpoints determines the geometry chosen and the class of the result.

## References

Shurtz, Robert F., 2003. Compositional geometry and mass conservation. Mathematical Geology 35 (8), 972–937.

### Examples

```
data(SimulatedAmounts)
ep <- aplus(rbind(c(2,1,2),c(2,2,1),c(1,2,2)))
dat <- endpointCoordinatesInv(acomp(sa.lognormals),acomp(ep))
plot(dat)
plot( acomp(endpointCoordinates(dat,acomp(ep))))
dat <- endpointCoordinatesInv(rcomp(sa.lognormals),rcomp(ep))
plot(dat)
plot( rcomp(endpointCoordinates(dat,rcomp(ep))))
dat <- endpointCoordinatesInv(aplus(sa.lognormals),aplus(ep))
plot(dat)
plot( endpointCoordinatesInv(rplus(sa.lognormals),rplus(ep))
plot(dat)
plot( endpointCoordinatesInv(rplus(sa.lognormals),rplus(ep))
plot(dat)
plot( endpointCoordinatesInv(rplus(sa.lognormals),rplus(ep))
plot(dat)
plot(endpointCoordinates(rplus(dat),rplus(ep)))</pre>
```

```
gsi2.invperm
```

## Internal function: Invert a permutation

### Description

Finds the inverse of a permutation given as a vector of indices.

## Usage

gsi2.invperm( i,n )

### Arguments

i	a sequence of different integers in 1:n considered as a permutation given
	<pre>by p=unique(c(i,1:n))</pre>
n	the number of elements to be permuted

## Details

The inverse permutation is defined by p[ var{v}]==1:n and v[ var{p}]==1:n.

## Value

an integer vector v describing the inverse permutation of p.

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## References

## See Also

gsi

# Examples

gsi2.invperm(c(2,3),10)

gsiinternal2 Internal functions of the compositions package

# Description

Internal functions

## Usage

gsi.pairrelativeMatrix(names)

## Arguments

names a character vector provinding names

# Details

## Value

a matrix containing pairwise contrasts

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

gsi

```
gsi.pairrelativeMatrix(c("a","b","c"))
```

rmultarithm

## Description

vector space operations computed for multiple vectors in parallel

#### Usage

```
## Methods for class "rmult"
## x+y
## x-y
## -x
## x*r
## r*x
## r*x
## x/r
```

#### Arguments

х	an rmult vector or dataset of vectors
У	an rmult vector or dataset of vectors
r	a numeric vector of size 1 or $\operatorname{nrow}(\mathbf{x})$

## Details

The operators try to mimic the parallel operation of R on vectors of real numbers on vectors of vectors represented as matrices containing the vectors as rows.

## Value

an object of class "rmult" containing the result of the corresponding operation on the vectors.

## See Also

rmult, %\*%.rmult

```
x <- rmult(matrix( sqrt(1:12), ncol= 3 ))
x
x+x
x + rmult(1:3)
x * 1:4
1:4 * x
x / 1:4
x / 10</pre>
```

## Description

Compute the isometric identity transform of a vector (dataset) of amounts and its inverse.

#### Usage

iit( x )
iit.inv( z )

#### Arguments

x	a vector or data matrix of amounts
Z	the iit-transform of a vector or data.matrix of iit-transforms of amounts

## Details

The iit-transform maps D amounts (considered in a real geometry) isometrically to a D dimensional euclidian vector. The iit is part of the **rplus** framework. Despite its trivial operation, it is present to achieve maximal analogy between the **aplus** and the **rplus** framework.

The data can then be analysed in this transformated space by all classical multivariate analysis tools. The interpretation of the results is easy since the relation to the original variables is preserved. However results may be inconsistent, since the multivariate analysis tools disregard the positivity condition and the inner laws of amounts.

The isometric identity transform is a simple identity given by

$$iit(x)_i := x_i$$

### Value

ilt gives the isometric identity transform, i.e. simply the input striped of the "rplus" class attribute, ipt.inv gives amounts with class "rplus" with the given iit, i.e. simply the argument checked to be a valid "rplus" object, and with this class attribute.

## Note

iit can be used to unclass amounts.

# References

#### iit

#### See Also

ilt, ilr, rplus

### Examples

```
(tmp <- iit(c(1,2,3)))
iit.inv(tmp)
iit.inv(tmp) - c(1,2,3) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(iit(cdata))
```

gsi.mapinO1 Internal functions: Storing integers as reals

#### Description

An integer number is stored in a dataset with a given range.

#### Usage

```
gsi.mapin01(i,min=0,max=1)
gsi.mapfrom01(x)
gsi.mapmin(x)
gsi.mapmax(x)
```

#### Arguments

```
i
x
max
min
```

the minimum of the created dataset

## Details

The function is used to get full control over the graphic ranges in pair plots and to pass the used column to panel functions.

# Value

```
gsi.mapin01 gives a vector x with range(
var{x})==c(min,max) and gsi.mapfrom01(
var{x}), gsi.mapmin(
var{x}), gsi.mapmax(
var{x}) result in i, max and min.
```

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

## See Also

 $\tt gsi, \tt plot.acomp$ 

## Examples

gsi.mapin01(5)

gsiinternal3 Internal functions of the compositions package

# Description

Internal functions

# Usage

gsi.spreadToIsoSpace(spread)

## Arguments

spread a matrix or a dataset of matrices

## Details

## Value

Converts a clr covariance matrix to a ilr covariance matrix

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi

gsi.textpanel

# Description

A function useful as a text.panel in pairs.

# Usage

gsi.textpanel(x,y,lab,...)

## Arguments

x	discarded
у	discarded
lab	text to be plotted to the middle of the panel
	further graphical parameters passed to <code>text</code>

## Details

The function is used against log-scale problems in pairs called by function **boxplot.acomp**.

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

# See Also

# gsi

# Examples

data(iris)
pairs(iris,text.panel=gsi.textpanel)

split

 $Spliting \ datasets \ in \ groups \ given \ by \ factors$ 

## Description

Each of the given scale levels has an associated norm, which is computed for each element by these functions.

#### Usage

```
## S3 method for class 'acomp':
split(x,f)
## S3 method for class 'rcomp':
split(x,f)
## S3 method for class 'aplus':
split(x,f)
## S3 method for class 'rplus':
split(x,f)
## S3 method for class 'rmult':
split(x,f)
```

# Arguments

х	a dataset or a single vector of some type
f	a factor that defines the grouping or a list of factors

# Value

a list of objects of the same type as x.

## See Also

#### split

# Examples

```
data(SimulatedAmounts)
split(acomp(sa.groups),sa.groups.area)
```

gsi.plain

Internal function: Convert to plain vector or matrix

# Description

The dataset is converted into a plain vector or matrix: data.frames are converted to data matrices and class attributes are removed.

## Usage

gsi.plain( x )

#### Arguments

x The dataset to be converted

# Details

# Value

unclassed object, typically a vector or matrix.

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

# References

## See Also

# Examples

gsi.plain(acomp(c(12,3,4)))

gsiinternal Internal functions of the compositions package

## Description

Internal functions

## Usage

gsi()

## Arguments

None

# Details

# Value

# Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi

## Examples

ilr

### Isometric log ratio transform

### Description

Compute the isometric log ratio transform of a (dataset of) composition(s) and its inverse.

#### Usage

ilr( x , V = ilrBase(x) )
ilr.inv( z , V = ilrBase(z=z))

### Arguments

x	a composition, not necessarily closed
z	the ilr-transform of a composition
V	a matrix, with columns giving the chosen basis of the clr-plane

## Details

The ilr-transform maps a composition in the D-part Aitchison-simplex isometrically to a D-1 dimensional euclidian vector. The data can then be analysed in this transformation by all classical multivariate analysis tools. However the interpretation of the results may be difficult, since there is no one-to-one relation between the original parts and the transformed variables.

The isometric logratio transform is given by

$$ilr(x) := V^t clr(x)$$

with clr(x) the centred log ratio transform and  $V \in R^{d \times (d-1)}$  a matrix which columns form an orthonormal basis of the clr-plane. A default matrix V is given by *ilrBase(var{D})*.

## Value

ilr gives the isometric log ratio transform, ilr.inv gives closed compositions with the given ilr-transforms

#### References

Egozcue J.J., V. Pawlowsky-Glahn, G. Mateu-Figueras and C. Barcel'o-Vidal (2003) Isometric logratio transformations for compositional data analysis. *Mathematical Geology*, **35**(3) 279-300

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

## See Also

clr,alr,apt, ilrBase, http://ima.udg.es/Activitats/CoDaWork03

#### Examples

```
(tmp <- ilr(c(1,2,3)))
ilr.inv(tmp)
ilr.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(ilr(cdata))
ilrBase(D=3)</pre>
```

ilt

Isometric log transform

#### Description

Compute the isometric log transform of a vector (dataset) of amounts and its inverse.

#### Usage

```
ilt( x )
ilt.inv( z )
```

#### Arguments

x	a vector or data matrix of amounts
z	the ilt-transform of a vector or data matrix of ilt-transforms of amounts

# Details

The ilt-transform maps D amounts (considered in log geometry) isometrically to a D dimensional euclidean vector. The ilt is part of the aplus framework.

The data can then be analysed in this transformation by all classical multivariate analysis tools. The interpretation of the results is easy since the relation to the original variables is preserved.

The isometric log transform is given by

 $ilt(x)_i := \ln x_i$ 

## Value

ilt gives the isometric log transform, i.e. simply the log of the argument, ilt.inv gives amounts with the given ilt, i.e. simple the exp of the argument

# References

```
See Also
```

ilr, iit, aplus

### Examples

```
(tmp <- ilt(c(1,2,3)))
ilt.inv(tmp)
ilt.inv(tmp) - c(1,2,3) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(ilt(cdata))</pre>
```

princomp.rcomp Principal component analysis for real compositions

### Description

A principal component analysis is done in real geometry (i.e. cpt-transform) of the simplex. Some gimics simplify the interpretation of the obtained components.

## Usage

```
## S3 method for class 'rcomp':
princomp(x,...,scores=TRUE)
## S3 method for class 'princomp.rcomp':
print(x,...)
## S3 method for class 'princomp.rcomp':
plot(x,y=NULL,...,
npcs=min(10,length(x$sdev)),
type=c("screeplot","variance","biplot","loadings","relative"),
main=NULL,
scale.sdev=1)
## S3 method for class 'princomp.rcomp':
predict(object,newdata,...)
```

## Arguments

х	an rcomp dataset (for princomp) or a result from princomp.rcomp
У	not used
scores	a logical indicating whether scores should be computed or not
npcs	the number of components to be drawn in the scree plot
type	type of the plot: "screeplot" is a lined screeplot, "variance" is a boxplot like screeplot, "biplot" is a biplot, "loadings" displays the loadings as a barplot
scale.sdev	The multiple of sigma to use plotting the loadings
main	headline of the plot
object	a fitted princomp.rcomp object
newdata	another compositional dataset of class rcomp
	further arguments to pass to internally-called functions

#### Details

Mainly a princomp(cpt(x)) is performed. To avoid confusion the meaningless last principal component is removed.

The plot routine provides screeplots (type = "s",type= "v"), biplots (type = "b"), plots of the effect of loadings (type = "b") in scale.sdev\*sdev-spread, and loadings of pairwise differences (type = "r").

The interpretation of a screeplot does not differ from ordinary screeplots. It shows the eigenvalues of the covariance matrix, which represent the portions of variance explained by the principal components.

The interpretation of the biplot differs from classical one. The relevant variables are not the drawn arrows of the components, but rather the differences between two arrowheads, which can be interpreted as transfer of mass from one component to the other.

The compositional loading plot is more or less a standard one. The loadings are displayed by a barplot as positve and negative changes of amounts.

The loading plot can work in two different modes: If scale.sdev is set to NA it displays the composition being represented by the unit vector of loadings in cpt-transformed space. If scale.sdev is numeric we use this composition scaled by the standard deviation of the respective component.

The relative plot displays the **relativeLoadings** as a barplot. The deviation from a unit bar shows the effect of each principal component on the respective differences.

### Value

princomp gives an object of type c("princomp.rcomp", "princomp") with the following content:

sdev	the standard deviation of the principal components.
loadings	the matrix of variable loadings (i.e., a matrix which columns contain the eigenvectors). This is of class "loadings". The last eigenvalue is removed since it should contain the irrelevant scaling.
Loadings	The loadings as an rmult-object

center	the cpt-transformed vector of means used to center the dataset	
Center	the <b>rcomp</b> vector of means used to center the dataset	
scale	the scaling applied to each variable	
n.obs	number of observations	
scores	if <b>scores</b> = TRUE, the scores of the supplied data on the principal com- ponents and the information available. Scores are coordinates in a basis given by the principal components and thus not compositions	
call	the matched call	
na.action	not clearly understood	

predict returns a matrix of scores of the observations in the newdata dataset . The other routines are mainly called for their side effect of plotting or printing and return the object x.

#### See Also

cpt,rcomp, relativeLoadings princomp.acomp, princomp.rplus,

#### Examples

```
data(SimulatedAmounts)
pc <- princomp(rcomp(sa.lognormals5))</pre>
рс
summary(pc)
plot(pc)
                   #plot(pc,type="screeplot")
plot(pc,type="v")
plot(pc,type="biplot")
plot(pc,choice=c(1,3),type="biplot")
plot(pc,type="loadings")
plot(pc,type="loadings",scale.sdev=-1) # Downward
plot(pc,type="relative",scale.sdev=NA) # The directions
plot(pc,type="relative",scale.sdev=1) # one sigma Upward
plot(pc,type="relative",scale.sdev=-1) # one sigma Downward
biplot(pc)
screeplot(pc)
loadings(pc)
relativeLoadings(pc,mult=FALSE)
relativeLoadings(pc)
relativeLoadings(pc,scale.sdev=1)
relativeLoadings(pc,scale.sdev=2)
pc$sdev^2
```

cov(predict(pc,sa.lognormals5))

#### Description

Compute the centered default transform of a (dataset of) composition or amount.

#### Usage

```
cdt(x)
## Default S3 method:
cdt( x )
## S3 method for class 'acomp':
cdt( x )
## S3 method for class 'rcomp':
cdt( x )
## S3 method for class 'aplus':
cdt( x )
## S3 method for class 'rplus':
cdt( x )
## S3 method for class 'rmult':
cdt( x )
## S3 method for class 'factor':
cdt( x )
```

### Arguments

х

a classed amount or composition (or a matrix of), to be transformed with its centered default transform

## Details

The general idea of this package is to analyse the same data with different geometric concepts as similar as possible. For each of the four concepts there exists a unique transform expressing the geometry in a linear subspace, keeping the relation to the variables. This unique transformation is computed by cdt. For acomp the transform is clr, for rcomp it is cpt, for aplus it is ilt, and for rplus it is iit. Each component of the result is identified with a unit vector in the direction of the corresponding component of the original composition or amount. Keep in mind that the transform is not necessarily surjective and thus variances in the image space might be singular.

# Value

A corresponding matrix or vector containing the transforms.

### References

cdt

#### See Also

idt, clr, cpt, ilt, iit

## Examples

```
## Not run:
# the cdt is defined by
cdt <- function(x) UseMethod("cdt",x)
cdt.default <- function(x) x
cdt.acomp <- clr
cdt.rcomp <- cpt
cdt.aplus <- ilt
cdt.rplus <- iit
## End(Not run)
cdt(acomp(1:5))
cdt(rcomp(1:5))
```

var.acomp

Variances and covariances of amounts and compositions

#### Description

Compute the (co)variance matrix in the several approaches of compositional and amount data analysis.

#### Usage

```
var(x,...)
      ## Default S3 method:
      var(x, y=NULL, na.rm=FALSE, use, ...)
      ## S3 method for class 'acomp':
      var(x,y=NULL,...)
      ## S3 method for class 'rcomp':
      var(x,y=NULL,...)
      ## S3 method for class 'aplus':
      var(x,y=NULL,...)
      ## S3 method for class 'rplus':
      var(x,y=NULL,...)
      ## S3 method for class 'rmult':
      var(x,y=NULL,...)
      cov(x, y=x, ...)
      ## Default S3 method:
      cov(x, y=NULL, use="all.obs", method=c("pearson",
"kendall", "spearman"), ...)
      ## S3 method for class 'acomp':
      cov(x,y=NULL,...)
      ## S3 method for class 'rcomp':
```

```
cov(x,y=NULL,...)
## S3 method for class 'aplus':
cov(x,y=NULL,...)
## S3 method for class 'rplus':
cov(x,y=NULL,...)
## S3 method for class 'rmult':
cov(x,y=NULL,...)
```

# Arguments

х	a dataset, eventually of amounts or compositions
У	a second dataset, eventually of amounts or compositions
na.rm	see var
use	see var
method	see cov
	further arguments to var e.g. use

### Details

The basic functions of var, cov are turned to S3-generics. The original versions are copied to the default method. This allows us to introduce generic methods to handle variances and covariances of other datatypes such as amounts or compositions.

If classed amounts or compositions are involved, they are transformed with their corresponding transforms, using the centered default transform (cdt). That implies that the variances have to be interpreded in a log scale level for acomp and aplus.

We should be aware that variance matrices of compositions are singular. They can be transformed to the correponding nonsingular variances of ilr or ipt -space by clrvar2ilr.

In R versions older than v2.0.0, var and cov were defined in package "base" instead of in "stats". This might produce some misfunction.

# Value

The variance matrix of x or the covariance matrix of x and y.

# See Also

cdt, clrvar2ilr, clo, mean.acomp, acomp, rcomp, aplus, rplus, variation

```
data(SimulatedAmounts)
mean.col(sa.lognormals)
var(acomp(sa.lognormals))
var(rcomp(sa.lognormals))
var(aplus(sa.lognormals))
var(rplus(sa.lognormals))
```

```
cov(acomp(sa.lognormals5[,1:3]),acomp(sa.lognormals5[,4:5]))
cov(rcomp(sa.lognormals5[,1:3]),rcomp(sa.lognormals5[,4:5]))
cov(aplus(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
cov(rplus(sa.lognormals5[,1:3]),rplus(sa.lognormals5[,4:5]))
cov(acomp(sa.lognormals5[,1:3]),aplus(sa.lognormals5[,4:5]))
```

```
svd(var(acomp(sa.lognormals)))
```

rcomp	Compositions as	elements	of the	Simplex	embedded	in	the	D-
	dimensional real	space						

### Description

A class providing a way to analyse compositions in the philosophical framework of the Simplex as subset of the  $\mathbb{R}^{D}$ .

#### Usage

rcomp(X,parts=1:NCOL(oneOrDataset(X)),total=1)

#### Arguments

Х	composition or dataset of compositions
parts	vector containing the indices xor names of the columns to be used
total	the total amount to be used, typically 1 or 100

#### Details

Many multivariate datasets essentially describe amounts of D different parts in a whole. This has some important implications justifying to regard them as a scale on its own, called a composition. The functions around the class "rcomp" follow the traditional (but statistically inconsistent) approach regarding compositions simply as a multivariate vector of positive numbers summing up to 1. This space of D positive numbers summing to 1 is traditionally called the D-1-dimensional simplex.

The compositional scale was in-depth analysed by Aitchison (1986) and he found serious reasons why compositional data should be analysed with a different geometry. The functions around the class "acomp" follow his approach. However the Aitchison approach based on logratios is sometimes criticized (e.g. Rehder and Zier, 2002). It cannot deal with absent parts (i.e. zeros). It is sensitive to large measurement errors in small amounts. The Aitchison operations cannot represent simple mixture of different chemical compositions. The used transformations are not uniformly continuous. Straight lines and ellipses in Aitchison space look strangely in ternary diagrams. As all uncritical statistical analysis, blind application of logratio-based analysis is sometimes misleading. Therefore it is sometimes usefull to analyse compositional data directly as a multivariate dataset of portions summing to 1. However a clear warning must be given that the utilisation of almost any kind of classical multivariate analysis introduce some kinds of artifacts (e.g. Chayes 1960) when applied to compositional data. So extra care and considerable expert knowlegde is needed for the proper interpretation of results achieved in this non-Aitchison approach. The package tries to lead the user around these artifacts as much as possible and gives hints to major pitfalls in the help. However meaningless results cannot be fully avoided in this (rather inconsistent) approach.

A side effect of the procedure is to force the compositions to sum to one, which is done by the closure operation clo.

The classes rcomp, acomp, aplus, and rplus are designed in a fashion as similar as possible, in order to allow direct comparison between results achieved by the different approaches. Especially the acomp logistic transforms clr, alr, ilr are mirrored by analogous linear transforms cpt, apt, ipt in the rcomp class framework.

## Value

a vector of class "rcomp" representing a closed composition or a matrix of class "rcomp" representing multiple closed compositions, by rows.

#### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

Rehder, S. and U. Zier (2001) Letter to the Editor: Comment on "Logratio Analysis and Compositional Distance" by J. Aitchison, C. Barceló-Vidal, J.A. Martín-Fernández and V. Pawlowsky-Glahn, *Mathematical Geology*, **33** (7), 845-848.

Zier, U. and S. Rehder (2002) Some comments on log-ratio transformation and compositional distance, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

# See Also

cpt, apt, ipt, acomp, rplus, princomp.rcomp, plot.rcomp, boxplot.rcomp, barplot.rcomp, mean.rcomp, var.rcomp, variation.rcomp, cov.rcomp, msd, convex.rcomp, +.rcomp

```
data(SimulatedAmounts)
plot(rcomp(sa.tnormals))
```

plot.acomp

# Description

# Usage

```
## S3 method for class 'acomp':
plot(x,...,labels=colnames(X),cn=colnames(X),aspanel=FALSE,id=FALSE,idlabs=NULL,idcol=2,center=
## S3 method for class 'rcomp':
plot(x,...,labels=colnames(X),cn=colnames(X),aspanel=FALSE,id=FALSE,idlabs=NULL,idcol=2,center=
```

## Arguments

x	a dataset of a compositional class
	further graphical parameters passed (see par)
margin	The type of marginalisation to be computed, when displaying the individ- ual panels. Possible values are: "acomp", "rcomp" and any of the variable names/column numbers in the composition. If one of the columns is se- lected each panel displays a subcomposition given by the row part, the column part and the given part. If one of the classes is given the corre- sponding margin acompmargin or rcompmargin is used.
add	a logical indicating whether the information should just be added to an existing plot. In case of false a new plot is created.
triangle	A logical indicating whether the triangle should be drawn.
col	The color to plot the data.
labels	The names of the parts
cn	The names of the parts to be used in a single panel. Internal use only.
aspanel	Logical indicating that only a single panel should be drawn and not the whole plot. Internal use only.
id	A logical. If true one can identify the points like with the <b>identify</b> command.
idlabs	A character vector providing the labels to be used with the identification, when $\mathtt{id=TRUE}$
idcol	color of the idlabs-labels
center	a logical indicating whether a the data should be centered prior to the plot. Centering is done in the choosen philosophy. See scale
scale	a logical indicating whether a the data should be scaled prior to the plot. Scaling is done in the choosen philosophy. See scale

pca	A logical indicating whether the first principle component should be dis-
	played in the plot. Currently direction of the principle component of the
	displayed subcomposition is displayed as a line. Later on a the principle
	componenent of the whole dataset should be displayed.
col.pca	The color to draw the principle component.

#### Details

The data is displayed in ternary diagrams. This does not work for two part compositions. Compositions of three parts are displayed in a single ternary diagram. For compositions of more than three components, the data is arrange in a scatterplot matrix through the command **pairs**.

The third component in each of the panels is than choosen according to setting of margin=. Possible values of margin= are: "acomp", "rcomp" and any of the variable names/column numbers in the composition. If one of the columns is selected each panel displays a sub-composition given by the row part, the column part and the given part. If one of the classes is given the corresponding margin acompmargin or rcompmargin is used.

Ternary diagrams can be read in multiple ways. Each corner of the triangle corresponds to a composition only containing the single part displayed in that corner. Points on the edges correspond to compositions only containing the parts in the adjacent corners. The relative amounts are displayed by the distance to the opposite corner. The individual portions of general points can be inferred by imaginatorily drawing a line parallel to the edge opposite to the corner of the part of interest through the point. The portion of the part of intrest is constant along the line. Thus we can read it on both crossing points of the line with the edges.

Relative portions of two parts can be inferred by imaginatorily drawing a line through the point and the corner of the unimportant component. This line intersects the edge between the two components of interest in the composition with the same relative portion of the two remaining components.

Exactly the lines parallel to one of the edges or going through one of the corners are straight lines as well in Aitchison and as in real geometry. They remain straight under an arbitrary perturbation.

#### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

Billheimer, D., P. Guttorp, W.F. and Fagan (2001) Statistical interpretation of species composition, *Journal of the American Statistical Association*, **96** (456), 1205-1214

Pawlowsky-Glahn, V. and J.J. Egozcue (2001) Geometric approach to statistical analysis on the simplex. *SERRA* **15**(5), 384-398

http://ima.udg.es/Activitats/CoDaWork03

http://ima.udg.es/Activitats/CoDaWork05

## See Also

plot.aplus, qqnorm.acomp,boxplot.acomp

## Examples

```
data(SimulatedAmounts)
plot(acomp(sa.lognormals))
plot(rcomp(sa.lognormals))
plot(acomp(sa.lognormals5),pca=TRUE)
plot(rcomp(sa.lognormals5),pca=TRUE)
```

```
ipt
```

Isometric planar transform

#### Description

Compute the isometric planar transform of a (dataset of) composition(s) and its inverse.

#### Usage

ipt( x , V = ilrBase(x) )
ipt.inv( z , V = ilrBase(z=z) )
ucipt.inv( z , V = ilrBase(z=z) )

## Arguments

х	a composition or a data matrix of compositions, not necessarily closed
Z	the ipt-transform of a composition or a data matrix of ipt-transforms of compositions
V	a matrix with columns giving the chosen basis of the clr-plane

# Details

The ipt-transform maps a composition in the D-part real-simplex isometrically to a D-1 dimensional euclidian vector. Although the transformation does not reach the whole  $R^{D-1}$ , resulting covariance matrices are typically of full rank.

The data can then be analysed in this transformation by all classical multivariate analysis tools. However, interpretation of results may be difficult, since the transform does not keep the variable names, given that there is no one-to-one relation between the original parts and each transformed variables. See cpt and apt for alternatives.

The isometric planar transform is given by

$$ipt(x) := V^t cpt(x)$$

with cpt(x) the centred planar transform and  $V \in R^{d \times (d-1)}$  a matrix which columns form an orthonormal basis of the clr-plane. A default matrix V is given by *ilrBase( var{D}*)

# Value

ipt gives the centered planar transform, ipt.inv gives closed compositions with with the given ipt-transforms, ucipt.inv unconstrained ipt.inv does the same as ipt.inv but sets illegal values to NA rather then giving an error. This is a workaround to allow procedures not honoring the constraints of the space.

## References

# See Also

ilr, ilr Base, cpt

# Examples

```
(tmp <- ipt(c(1,2,3)))
ipt.inv(tmp)
ipt.inv(tmp) - clo(c(1,2,3)) # 0
data(Hydrochem)
cdata <- Hydrochem[,6:19]
pairs(ipt(cdata))</pre>
```

gsicall

Internal functions of the compositions package

## Description

Calls a function with a list of arguments.

### Usage

gsi.call(fkt,...)

### Arguments

fkt	The function to be called
	The arguments to call the function with

# Details

This is only useful in conjunction with do.call and allows to call anonymous functions with a parameters given by a list.

### Value

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

#### See Also

gsi

#### Examples

```
mypars <- list(x=3)
do.call("gsi.call",c(list(function(x){x}),mypars))</pre>
```

Simulated Amounts Simulated amount datasets

## Description

Several simulated datasets intended as reference examples for various conceptual and statistical models of compositions and amounts.

# Usage

```
data(SimulatedAmounts)
```

## Format

Data matrices with 60 cases and 3 or 5 variables.

## Details

The statistical analysis of amounts and compositions is set to discussion. Four essentially different approaches are provided in this package around the classes "rplus", "aplus", "rcomp", "acomp". There is no absolutely "right" approach, since there is a conection between these approaches and the processes originating the data. We provide here simulated standard datasets and the corresponding simulation procedures following these several models to provide "good" analysis examples and to show how these models actually look like in data. The data sets are simulated according to correlated lognormal distributions (sa.lognormals, sa.lognormal5), winsorised correlated normal distributions (sa.tnormals, sa.tnormal5), Dirichlet distribution on the simplex (sa.dirichlet, sa.dirichlet5), uniform distribution on the simplex (sa.uniform, sa.uniform5), and a grouped dataset (sa.groups, sa.groups5) with three groups (given in sa.groups.area and sa.groups5.area) all distributed accordingly with a lognormal distribution with group dependent means.

We can imagine that amounts evolve in nature e.g. in part of the soil they are diluted and transported in a transport medium, usually water, which comes from independent source (the rain, for instance) and this new composition is normalized by taking a sample of standard size. For each of the datasets sa.X there is a corresponding sa.X.dil dataset which is build by simulating exactly that process on the corresponding sa.X dataset. The amounts in the sa.X.dil are given in ppm. This idea of a transport medium is a major argument for a compositional approach, because the total amount given by the sum of the parts is induced by the dilution given by the medium and thus uninformative for the original investigated process.

If we imagine now these amounts flowing into a river and sedimenting, the different contributions are accumulated along the river and renormalized to a unit portion on taking samples again. For each of the dataset sa.X.dil there is a corresponding sa.X.mix dataset which is build from the corresponding sa.X dataset by simulating exactly that accumulation process. Mixing of different compositions is a major argument against the log based approaches (aplus, acomp) since mixing is a highly nonlinear operation in terms of the logratios.

#### Source

The datasets are simulated for this package and are under the GNU Public Library Licence Version 2 or newer.

## References

http://statistic.boogaart.de/compositions/data

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

### Zier Rehder

xxx Something recommending to use log-transforms

xxx Something warning against log-transforms

```
data(SimulatedAmounts)
plot.acomp(sa.lognormals)
plot.acomp(sa.lognormals.dil)
plot.acomp(sa.lognormals.mix)
```

```
plot.acomp(sa.lognormals5)
plot.acomp(sa.lognormals5.dil)
plot.acomp(sa.lognormals5.mix)
library(MASS)
plot.rcomp(sa.tnormals)
plot.rcomp(sa.tnormals.dil)
plot.rcomp(sa.tnormals.mix)
plot.rcomp(sa.tnormals5)
plot.rcomp(sa.tnormals5.dil)
plot.rcomp(sa.tnormals5.mix)
plot.acomp(sa.groups,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.groups.dil,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.groups.mix,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.groups5,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.groups5.dil,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.groups5.mix,col=as.numeric(sa.groups.area),pch=20)
plot.acomp(sa.uniform)
plot.acomp(sa.uniform.dil)
plot.acomp(sa.uniform.mix)
plot.acomp(sa.uniform5)
plot.acomp(sa.uniform5.dil)
plot.acomp(sa.uniform5.mix)
plot.acomp(sa.dirichlet)
plot.acomp(sa.dirichlet.dil)
plot.acomp(sa.dirichlet.mix)
plot.acomp(sa.dirichlet5)
plot.acomp(sa.dirichlet5.dil)
plot.acomp(sa.dirichlet5.mix)
# The data was simulated with the following commands:
library(MASS)
dilution <- function(x) {clo(cbind(x,exp(rnorm(nrow(x),5,1))))[,1:ncol(x)]*1E6}
seqmix <- function(x) {clo(apply(x,2,cumsum))*1E6}</pre>
vars <- c("Cu","Zn","Pb")</pre>
vars5 <- c("Cu","Zn","Pb","Cd","Co")</pre>
sa.lognormals <- structure(exp(matrix(rnorm(3*60),ncol=3) %*%</pre>
                                chol(matrix(c(1,0.8,-0.2,0.8,1,
                                              -0.2,-0.2,-0.2,1),ncol=3))+
                                matrix(rep(c(1:3),each=60),ncol=3)),
                            dimnames=list(NULL,vars))
plot.acomp(sa.lognormals)
pairs(sa.lognormals)
sa.lognormals.dil <- dilution(sa.lognormals)</pre>
plot.acomp(sa.lognormals.dil)
```

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```

```
pairs(sa.lognormals.dil)
sa.lognormals.mix <- seqmix(sa.lognormals.dil)</pre>
plot.acomp(sa.lognormals.mix)
pairs(sa.lognormals.mix)
sa.lognormals5 <- structure(exp(matrix(rnorm(5*60),ncol=5) %*%</pre>
                                 chol(matrix(c(1,0.8,-0.2,0,0,
                                               0.8, 1, -0.2, 0, 0,
                                               -0.2, -0.2, 1, 0, 0,
                                               0, 0, 0, 5, 4.9,
                                               0,0,0,4.9,5),ncol=5))+
                                 matrix(rep(c(1:3,-2,-2),each=60),ncol=5)),
                            dimnames=list(NULL,vars5))
plot.acomp(sa.lognormals5)
pairs(sa.lognormals5)
sa.lognormals5.dil <- dilution(sa.lognormals5)</pre>
plot.acomp(sa.lognormals5.dil)
pairs(sa.lognormals5.dil)
sa.lognormals5.mix <- seqmix(sa.lognormals5.dil)</pre>
plot.acomp(sa.lognormals5.mix)
pairs(sa.lognormals5.mix)
sa.groups.area <- factor(rep(c("Upper","Middle","Lower"),each=20))</pre>
sa.groups <- structure(exp(matrix(rnorm(3*20*3),ncol=3) %*%</pre>
                                 chol(0.5*matrix(c(1,0.8,-0.2,0.8,1,
                                               -0.2,-0.2,-0.2,1),ncol=3))+
                                 matrix(rep(c(1,2,2.5,2,2.9,5,4,2,5),
                                            each=20),ncol=3)),
                            dimnames=list(NULL,c("clay","sand","gravel")))
plot.acomp(sa.groups,col=as.numeric(sa.groups.area),pch=20)
pairs(sa.lognormals,col=as.numeric(sa.groups.area),pch=20)
sa.groups.dil <- dilution(sa.groups)</pre>
plot.acomp(sa.groups.dil,col=as.numeric(sa.groups.area),pch=20)
pairs(sa.groups.dil,col=as.numeric(sa.groups.area),pch=20)
sa.groups.mix <- seqmix(sa.groups.dil)</pre>
plot.acomp(sa.groups.mix,col=as.numeric(sa.groups.area),pch=20)
pairs(sa.groups.mix,col=as.numeric(sa.groups.area),pch=20)
sa.groups5.area <- factor(rep(c("Upper","Middle","Lower"),each=20))</pre>
sa.groups5 <- structure(exp(matrix(rnorm(5*20*3),ncol=5) %*%</pre>
                                 chol(matrix(c(1,0.8,-0.2,0,0,
                                               0.8, 1, -0.2, 0, 0,
                                               -0.2,-0.2,1,0,0,
                                               0,0,0,5,4.9,
```

```
0,0,0,4.9,5,ncol=5))+
                                matrix(rep(c(1,2,2.5,
                                              2,2.9,5,
                                              4,2.5,0,
                                              -2, -1, -1,
                                              -1, -2, -3),
                                            each=20),ncol=5)),
                            dimnames=list(NULL,
                              vars5))
plot.acomp(sa.groups5,col=as.numeric(sa.groups5.area),pch=20)
pairs(sa.groups5,col=as.numeric(sa.groups5.area),pch=20)
sa.groups5.dil <- dilution(sa.groups5)</pre>
plot.acomp(sa.groups5.dil,col=as.numeric(sa.groups5.area),pch=20)
pairs(sa.groups5.dil,col=as.numeric(sa.groups5.area),pch=20)
sa.groups5.mix <- seqmix(sa.groups5.dil)</pre>
plot.acomp(sa.groups5.mix,col=as.numeric(sa.groups5.area),pch=20)
pairs(sa.groups5.mix,col=as.numeric(sa.groups5.area),pch=20)
sa.tnormals <- structure(pmax(matrix(rnorm(3*60),ncol=3) %*%</pre>
                                chol(matrix(c(1,0.8,-0.2,0.8,1,
                                               -0.2,-0.2,-0.2,1),ncol=3))+
                                matrix(rep(c(0:2),each=60),ncol=3),0),
                            dimnames=list(NULL,c("clay","sand","gravel")))
plot.rcomp(sa.tnormals)
pairs(sa.tnormals)
sa.tnormals.dil <- dilution(sa.tnormals)</pre>
plot.acomp(sa.tnormals.dil)
pairs(sa.tnormals.dil)
sa.tnormals.mix <- seqmix(sa.tnormals.dil)</pre>
plot.acomp(sa.tnormals.mix)
pairs(sa.tnormals.mix)
sa.tnormals5 <- structure(pmax(matrix(rnorm(5*60),ncol=5) %*%</pre>
                                chol(matrix(c(1,0.8,-0.2,0,0,
                                              0.8,1,-0.2,0,0,
                                               -0.2,-0.2,1,0,0,
                                               0,0,0,0.05,0.049,
                                               0,0,0,0.049,0.05),ncol=5))+
                                matrix(rep(c(0:2,0.1,0.1),each=60),ncol=5),0),
                            dimnames=list(NULL,
                              vars5))
plot.rcomp(sa.tnormals5)
```

```
pairs(sa.tnormals5)
```

```
sa.tnormals5.dil <- dilution(sa.tnormals5)</pre>
plot.acomp(sa.tnormals5.dil)
pairs(sa.tnormals5.dil)
sa.tnormals5.mix <- seqmix(sa.tnormals5.dil)</pre>
plot.acomp(sa.tnormals5.mix)
pairs(sa.tnormals5.mix)
sa.dirichlet <- sapply(c(clay=0.2,sand=2,gravel=3),rgamma,n=60)</pre>
colnames(sa.dirichlet) <- vars</pre>
plot.acomp(sa.dirichlet)
pairs(sa.dirichlet)
sa.dirichlet.dil <- dilution(sa.dirichlet)</pre>
plot.acomp(sa.dirichlet.dil)
pairs(sa.dirichlet.dil)
sa.dirichlet.mix <- seqmix(sa.dirichlet.dil)</pre>
plot.acomp(sa.dirichlet.mix)
pairs(sa.dirichlet.mix)
sa.dirichlet5 <- sapply(c(clay=0.2,sand=2,gravel=3,humus=0.1,plant=0.1),rgamma,n=60)</pre>
colnames(sa.dirichlet5) <- vars5</pre>
plot.acomp(sa.dirichlet5)
pairs(sa.dirichlet5)
sa.dirichlet5.dil <- dilution(sa.dirichlet5)</pre>
plot.acomp(sa.dirichlet5.dil)
pairs(sa.dirichlet5.dil)
sa.dirichlet5.mix <- seqmix(sa.dirichlet5.dil)</pre>
plot.acomp(sa.dirichlet5.mix)
pairs(sa.dirichlet5.mix)
sa.uniform <- sapply(c(clay=1,sand=1,gravel=1),rgamma,n=60)</pre>
colnames(sa.uniform) <- vars</pre>
plot.acomp(sa.uniform)
pairs(sa.uniform)
sa.uniform.dil <- dilution(sa.uniform)</pre>
plot.acomp(sa.uniform.dil)
pairs(sa.uniform.dil)
sa.uniform.mix <- seqmix(sa.uniform.dil)</pre>
```

plot.acomp(sa.uniform.mix)
pairs(sa.uniform.mix)
```
sa.uniform5 <- sapply(c(clay=1,sand=1,gravel=1,humus=1,plant=1),rgamma,n=60)
colnames(sa.uniform5) <- vars5
plot.acomp(sa.uniform5)
pairs(sa.uniform5.dil <- dilution(sa.uniform5)
plot.acomp(sa.uniform5.dil)
pairs(sa.uniform5.dil)
sa.uniform5.mix <- seqmix(sa.uniform5.dil)
plot.acomp(sa.uniform5.mix)
pairs(sa.uniform5.mix)
objects(pattern="sa.*")</pre>
```

```
rlnorm
```

The multivariate lognormal distribution

#### Description

Generates random amounts with a multivariate lognormal distribution .

## Usage

rlnorm.rplus(n,meanlog,varlog)
dlnorm.rplus(x,meanlog,varlog)

#### Arguments

n	number of datasets to be simulated
meanlog	The mean-vector of the logs
varlog	The variance/covariance matrix of the logs
x	vectors in the sample space

# Value

rlnorm.rplus gives a generated random dataset of class "rplus" following a lognormal distribution with logs having mean meanlog and variance varlog. dlnorm.rplus gives the density of the distribution with respect to the Lesbesgue measure on R+ as a subset of R.

## Note

The main difference between rlnorm.rplus and rnorm.aplus is that rlnorm.rplus needs a loged mean. The additional difference for the calculation of the density by dlnorm.rplus and dnorm.aplus is the reference measure.

### References

Aitchison, J. (1986) *The Statistical Analysis of Compositional Data* Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

### See Also

rnorm.acomp

#### Examples

```
MyVar <- matrix(c(
0.2,0.1,0.0,
0.1,0.2,0.0,
0.0,0.0,0.2),byrow=TRUE,nrow=3)
MyMean <- c(1,1,2)
plot(rlnorm.rplus(100,log(MyMean),MyVar))
plot(rnorm.aplus(100,MyMean,MyVar))
x <- rnorm.aplus(5,MyMean,MyVar)
dnorm.rplus(x,MyMean,MyVar)
```

names

#### The names of the parts

## Description

The names function provide a transparent way to access the names of the parts regardless of the shape of the dataset or data item.

#### Usage

```
## S3 method for class 'acomp':
names(x)
## S3 method for class 'rcomp':
names(x)
## S3 method for class 'aplus':
names(x)
## S3 method for class 'rplus':
names(x)
## S3 method for class 'rmult':
names(x)
## S3 method for class 'acomp':
names(x) <- value
## S3 method for class 'rcomp':
names(x) <- value</pre>
```

```
## S3 method for class 'aplus':
names(x) <- value
## S3 method for class 'rplus':
names(x) <- value
## S3 method for class 'rmult':
names(x) <- value</pre>
```

# Arguments

х	an amount/amount dataset
value	the new names of the parts
•••	not used, only here for generics

## Value

a character vector giving the names of the parts

## See Also

aplus

# Examples

```
data(SimulatedAmounts)
tmp <- acomp(sa.lognormals)
names(tmp)
names(tmp) <- c("x","y","z")
tmp</pre>
```

groupparts

Group amounts of parts

### Description

Groups parts by amalgamation or balancing of their amounts or proportions.

## Usage

```
groupparts(x,...)
## S3 method for class 'acomp':
groupparts(x,...,groups=list(...))
## S3 method for class 'rcomp':
groupparts(x,...,groups=list(...))
## S3 method for class 'aplus':
groupparts(x,...,groups=list(...))
## S3 method for class 'rplus':
groupparts(x,...,groups=list(...))
```

#### Arguments

х	an amount/compositional dataset
	further parameters to use (actually ignored)
groups	a list of numeric xor character vectors, each giving a group of parts

### Details

In the real geometry grouping is done by amalgamation (i.e. adding the parts). In the Aitchison-geometry grouping is done by taking geometric means. The new parts are named by named formal arguments. Not-mentioned parts remain ungrouped.

## Value

a new dataset of the same type with each group represented by a single column

#### References

Egozcue, J.J. and V. Pawlowsky-Glahn (2005) Groups of Parts and their Balances in Compositional Data Analysis, Mathematical Geology, in press

#### See Also

aplus

## Examples

```
data(SimulatedAmounts)
groupparts(acomp(sa.lognormals5),A=c(1,2),B=c(3,4),C=5)
groupparts(aplus(sa.lognormals5),B=c(3,4),C=5)
groupparts(rcomp(sa.lognormals5),A=c("Cu","Pb"),B=c(2,5))
groupparts(rplus(sa.lognormals5),1:5)
```

aplusarithm vectorial arithmetic for datasets with aplus class

# Description

The positive vectors equipped with the perturbation (defined as the element-wise product) as Abelian sum, and powertransform (defined as the element-wise powering with a scalar) as scalar multiplication forms a real vector space. These vector space operations are defined here in a similar way to +.rmult.

## Usage

```
perturbe.aplus(x,y)
## Methods for aplus
## x+y
## x-y
## -x
## x*r
## r*x
## r*x
## x/r
power.aplus(x,r)
```

### Arguments

x	an aplus vector or dataset of vectors
У	an aplus vector or dataset of vectors
r	a numeric vector of size 1 or $\operatorname{nrow}(\mathbf{x})$

# Details

The operators try to mimic the parallel operation of R for vectors of real numbers to vectors of amounts, represented as matrices containing the vectors as rows and works like the operators for {rmult}

## Value

an object of class "aplus" containing the result of the corresponding operation on the vectors.

# See Also

rmult, %\*%.rmult

### Examples

```
x <- aplus(matrix( sqrt(1:12), ncol= 3 ))
x
x+x
x + aplus(1:3)
x * 1:4
1:4 * x
x / 1:4
x / 10
power.aplus(x,1:4)</pre>
```

gsi.getD

# Description

Get the number of samples N and the number of parts D of the compositions in an acomp, rcomp, aplus, rplus object.

#### Usage

gsi.getD(x)
gsi.getN(x)

### Arguments

x

an acomp, rcomp, aplus, rplus object or something that could be cast to one of them

## Value

an integer giving the number of parts D or the number of samples N.

## Note

Do not use gsi.\* functions directly since they are internal functions of the package

### Examples

```
gsi.getD(1:5)
gsi.getN(1:5)
NCOL(1:5)
NROW(1:5)
data(SimulatedAmounts)
gsi.getD(sa.lognormals5)
gsi.getN(sa.lognormals5)
```

mean.acomp

Mean amounts and mean compositions

### Description

Compute the mean in the several approaches of compositional and amount data analysis.

## Usage

```
mean.acomp(x,..., na.action=get(getOption("na.action")))
mean.rcomp(x,..., na.action=get(getOption("na.action")))
mean.aplus(x,..., na.action=get(getOption("na.action")))
mean.rplus(x,..., na.action=get(getOption("na.action")))
mean.rmult(x,..., na.action=get(getOption("na.action")))
```

### Arguments

x	a classed dataset of amounts or compositions
	further arguments to mean e.g. trim
na.action	The na.action to be used: one of na.omit,na.fail,na.pass

# Details

The different compositional approaches acomp, rcomp, aplus, rplus correpond to different geometries. The mean is calculated in the respective canonical geometry by applying a canonical transform (see cdt), taking ordinary mean.col and backtransforming.

The Aitchison geometries imply that mean.acomp and mean.aplus are geometric means, the first one closed. The real geometry implies that mean.rcomp and mean.rplus are arithmetic means, the first one resulting in a closed composition.

In all cases the mean is again an object of the same class.

## Value

The mean is given as a composition or amount vector of the same class as the original dataset.

## See Also

clo, mean.col, geometricmean, acomp, rcomp, aplus, rplus

## Examples

```
data(SimulatedAmounts)
mean.col(sa.lognormals)
mean(acomp(sa.lognormals))
mean(rcomp(sa.lognormals))
mean(aplus(sa.lognormals))
mean(rplus(sa.lognormals))
mean(rmult(sa.lognormals))
```

ilrBase

## Description

Compute the basis of a clr-plane, to use with isometric log-ratio or planar transform of a (dataset of) compositions.

#### Usage

ilrBase( x=NULL , z=NULL , D = NULL )
gsi.ilrBase(D)

## Arguments

х	optional dataset or vector of compositions
z	optional dataset or vector containing ilr or ipt coordinates
D	number of parts of the simplex

# Details

ilrBase is a wrapper catching the answers of gsi.ilrBase and is to be used as the more convenient function. Only one of the arguments is needs to determine the dimension of the simplex.

## Value

Both methods give a matrix containing by columns the basis elements for the canonical basis of the clr-plane used for the ilr and ipt transform.

#### References

Egozcue J.J., V. Pawlowsky-Glahn, G. Mateu-Figueras and C. Barcel'o-Vidal (2003) Isometric logratio transformations for compositional data analysis. *Mathematical Geology*, **35**(3) 279-300

## See Also

clr,ilr,ipt, http://ima.udg.es/Activitats/CoDaWork03

#### Examples

```
ilr(c(1,2,3))
ilrBase(D=2)
ilrBase(c(1,2,3))
ilrBase(z= ilr(c(1,2,3)) )
round(ilrBase(D=7),digits= 3)
```

## clr2ilr

Convert between clr and ilr, and between cpt and ipt. Acts in vectors and in bilinear forms.

# Description

Compute the centered log ratio transform of a (dataset of) isometric log-ratio transform(s) and its inverse. Equivalently, compute centered and isometric planar transforms from each other.

## Usage

```
clr2ilr( x , V=ilrBase(x) )
ilr2clr( z , V=ilrBase(z=z) )
clrvar2ilr( varx , V=ilrBase(D=ncol(varx)) )
ilrvar2clr( varz , V=ilrBase(D=ncol(varz)+1) )
```

## Arguments

X	the clr/cpt-transform of composition(s)
z	the ilr/ipt-transform of composition(s)
varx	variance or covariance matrix of $\rm clr/\rm cpt-transformed$ compositions
varz	variance or covariance matrix of ilr/ipt-transformed compositions $% \left( {{{\left[ {{{\left[ {{{\left[ {{{\left[ {{{\left[ {{{\left[ {{{\left[ {{{}}}} \right]}}} \right.}$
V	a matrix with columns giving the chosen basis of the clr-plane

## Details

These functions perform a matrix multiplication with V in an appropriate way.

## Value

clr2ilr gives the ilr/ipt transform of the same composition(s), ilr2clr gives the clr/cpt transform of the same composition(s), clrvar2ilr gives the variance-/covariance-matrix of the ilr/ipt transform of the same compositional data set, ilrvar2clr gives the variance-/covariance-matrix of the clr/cpt transform of the same compositional data set.

#### References

Egozcue J.J., V. Pawlowsky-Glahn, G. Mateu-Figueras and C. Barcel'o-Vidal (2003) Isometric logratio transformations for compositional data analysis. *Mathematical Geology*, **35**(3) 279-300

Aitchison, J, C. Barcel'o-Vidal, J.J. Egozcue, V. Pawlowsky-Glahn (2002) A consise guide to the algebraic geometric structure of the simplex, the sample space for compositional data analysis, *Terra Nostra*, Schriften der Alfred Wegener-Stiftung, 03/2003

## See Also

ilr, ipt

## Examples

```
data(SimulatedAmounts)
ilr.inv(clr2ilr(clr(sa.lognormals)))-clo(sa.lognormals)
clr.inv(ilr2clr(ilr(sa.lognormals)))-clo(sa.lognormals)
ilrvar2clr(var(ilr(sa.lognormals)))-var(clr(sa.lognormals))
clrvar2ilr(var(cpt(sa.lognormals)))-var(ipt(sa.lognormals)))
```

rcompmargin

Marginal compositions in real geometry

## Description

Compute marginal compositions by amalgamating the rest (additively).

#### Usage

```
rcompmargin(X,d=c(1,2),name="+",pos=length(d)+1)
```

#### Arguments

Х	composition or dataset of compositions
d	vector containing the indices xor names of the columns to be kept
name	The new name of the amalgamation column
pos	The position where the new amalgamation column should be stored. This defaults to the last column.

## Details

The amalgamation column is simply computed by adding the non-selected components after closing the composition. This is consistent with the **rcomp** approach and is widely used because of its easy interpretation. However, it often leads to difficult-to-read ternary diagrams and is inconsistent with the **acomp** approach.

## Value

A closed compositions with class "rcomp" containing the selected variables given by d and the the amalgamation column.

# References

#### See Also

acompmargin, rcomp

## Examples

```
data(SimulatedAmounts)
plot.rcomp(sa.tnormals5,margin="rcomp")
plot.rcomp(rcompmargin(sa.tnormals5,c("Cd","Zn")))
plot.rcomp(rcompmargin(sa.tnormals5,c(1,2)))
```

clo

Closure of a composition

### Description

Closes compositions to sum up to one (or an optional total), by dividing each part by the sum.

## Usage

```
clo( X, parts=1:NCOL(oneOrDataset(X)),total=1)
```

## Arguments

Х	composition or dataset of compositions
parts	vector containing the indices xor names of the columns to be used
total	the total amount to which the compositions should be closed; either a single number, or a numeric vector of length $gsi.getN(X)$ specifying a different total for each compositional vector in the dataset.

## Details

The closure operation is given by

$$clo(x) := \left(x_i / \sum_{j=1}^D x_j\right)$$

clo makes a composition without assigning one of the compositional classes acomp or rcomp. Note that after computing the closed-to-one version, obtaining a version closed to any other value is done by simple multiplication.

## Value

a composition or a datamatrix of compositions without compositional class. The individual compositions are forced to sum to 1 (or to the optionally-specified total). The result should have the same shape as the input (vector, row, matrix).

## Note

clo can be used to unclass compositions.

## References

Aitchison, J. (1986) The Statistical Analysis of Compositional Data Monographs on Statistics and Applied Probability. Chapman & Hall Ltd., London (UK). 416p.

## See Also

 $\tt clr, a \tt comp, r \tt comp$ 

### Examples

```
(tmp <- clo(c(1,2,3)))
clo(tmp,total=100)
data(Hydrochem)
cdata <- Hydrochem[,6:19]
plot( clo(Hydrochem,8:9) ) # Giving points on a line</pre>
```